

# PET : Quantitative imaging technology

Hokkaido University Hospital Department of  
Nuclear Medicine    Chietsugu Katoh, MD, Prof.

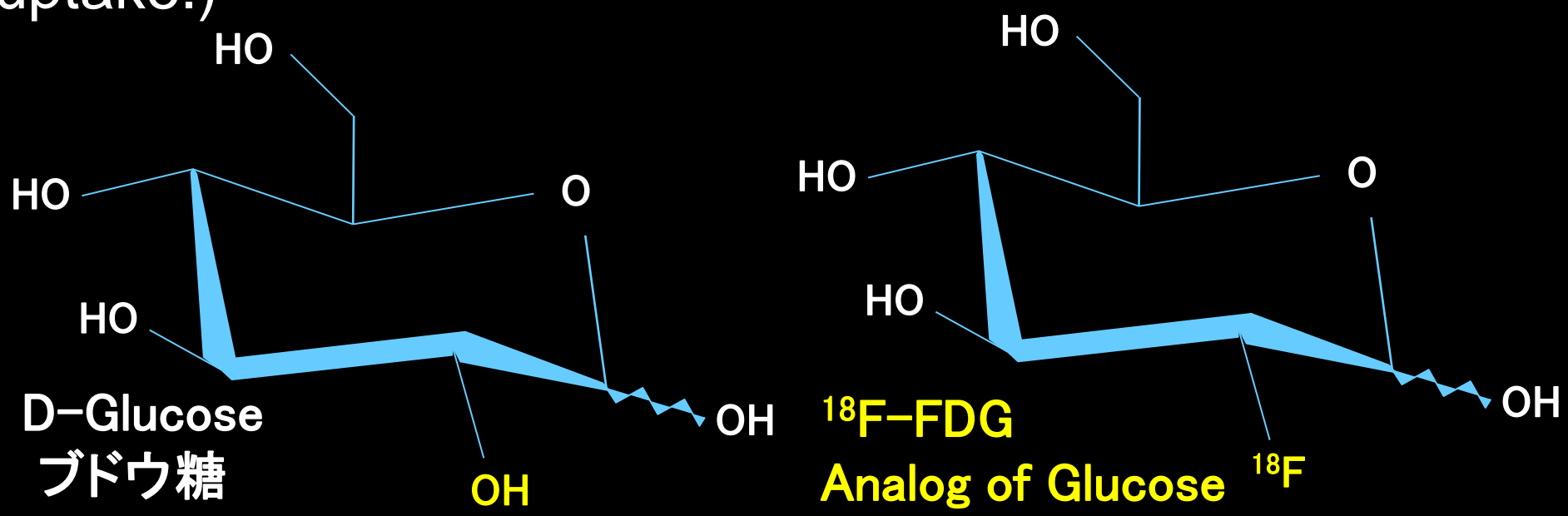
PET (Positron Emission Tomography):  
Radioactivity quantitative measurement  
device that calculates the distribution of  
positron emitting nuclides in the body in  
three dimensions and four dimensions

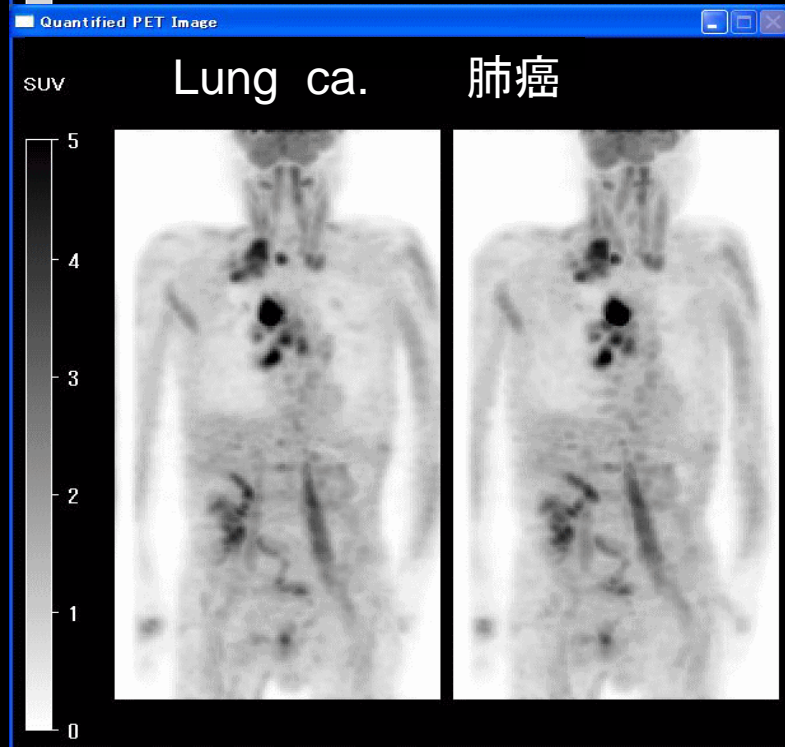
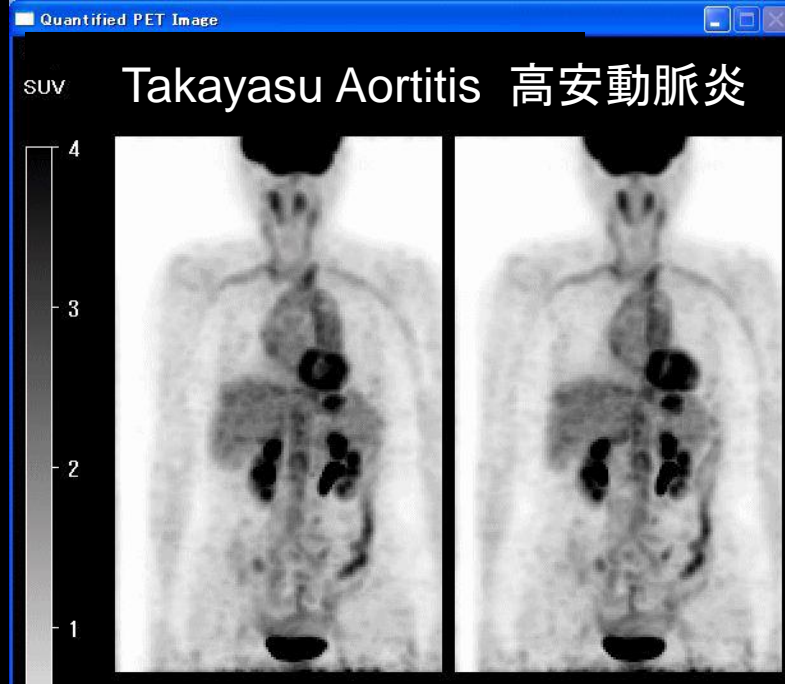
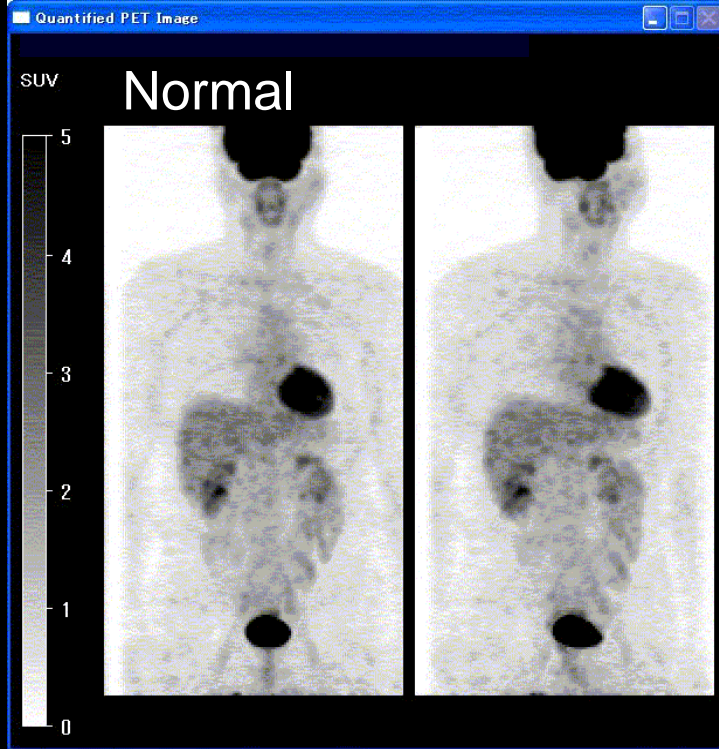
- High resolution (good image quality)
- High sensitivity
- Excellent quantification

$^{18}\text{F}$ -FDG (Fluoro Deoxy Glucose) is a substance similar to glucose, which is taken up by tissues like glucose, but is not metabolized, stays in the tissues for a long time, and is a useful drug for collecting glucose quantitative images of brain and lesions.

(However, it is difficult to be taken into hepatocytes and well-differentiated hepatocellular carcinoma.)

(Renal cancer clear cell carcinoma also has poor FDG uptake.)





$^{18}\text{F}$ -FDG PET  
Normal accumulation in  
the brain, urine, and  
sometimes myocardium,  
in addition to tumors  
and inflammation.

Generally, body tissues ingest **fatty acids** as an energy source and produce **ATP** (adenosine triphosphate) from the fatty acids in the **beta oxidation cycle** in mitochondria.

The beta oxidation cycle produces a lot of ATP but **requires a lot of oxygen**.

Abnormal tissues with high density of cells, such as cancer cells and inflammatory cells, **produce ATP in a glycolytic system** that does **not require much oxygen** because the blood vessels that are the passages of red blood cells that carry **oxygen are inadequate**.

Glycolysis produces a small amount of ATP, so **in normal tissues, glucose is not used very much**.

Then, FDG uptake shows the abnormal tissues.

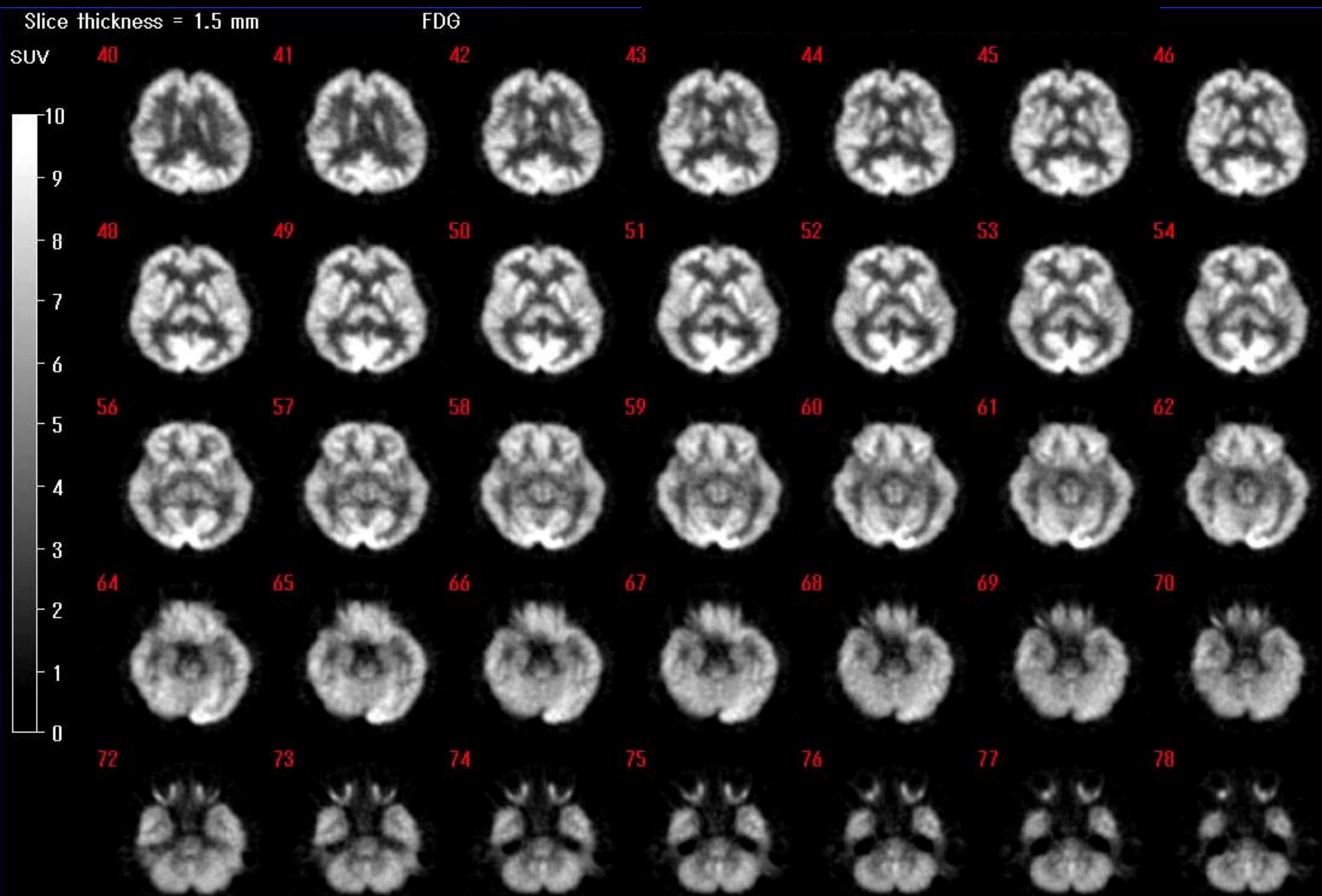
Hokkaido University Hospital  
Nuclear medicine laboratory  
**PET/CT装置**



**PET:**  
**陽電子CT**  
**Positron**  
**Emission CT**



# $^{18}\text{F}$ -FDG Brain PET 185MBq 1hour after i.v. 5min.



# Diseases covered by FDG-PET health insurance

1. **Epilepsy** (intractable, surgical indication)
2. **Ischemic heart disease** (diagnosis of viability)  
**Cardiac sarcoidosis** (fatal arrhythmia)
3. **Malignant tumor** (excluding early gastric ca.)  
(Cases judged to be malignant by **pathological** diagnosis, or by **other images** (CT, MRI, etc.).  
Evaluation of the therapeutic effect of **malignant lymphoma**.  
Patient with confirmed **metastasis**.)
4. Aortic inflammation  
(**Takayasu arteritis**, giant cell arteritis)

# Takayasu arteritis

One of the specified intractable diseases (with 330 diseases). 7,000 registered patients.

90% are women. The most common age is 10 to 30 years old. Young woman.

In a young woman with severe neck pain, headache, stiff shoulder, CT etc., findings such as stenosis in the branch vessels of the aortic arch.

If there is a difference between the left and right upper limb blood pressure measurement values, perform FDG PET / CT. FDG accumulation in inflamed blood vessels.

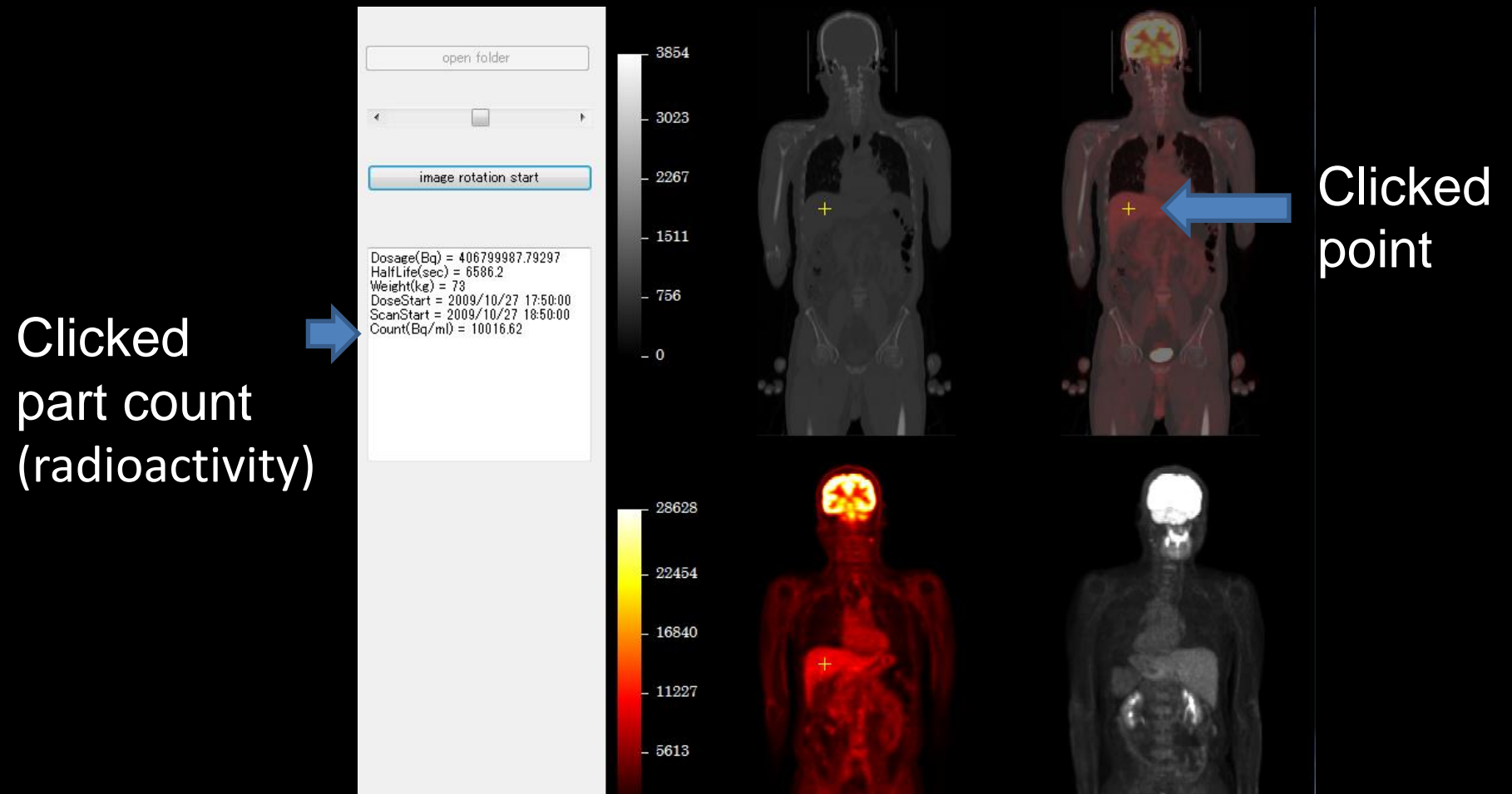
Treatment is steroids (relapses easily),

Antibody drug (tocilizumab (actemra) IL-6R

Originally rheumatoid arthritis. Expensive. 5000 yen /day



Click on any of the CT, PET and fusion images,  
The accumulation of the part is displayed.  
The clicked point is indicated by a yellow cross.



Calculate the SUV of the lesion from the FDG-PET image.

# SUV ( Standardized Uptake Value)

$$\text{SUV} = \frac{\text{Radioactivity concentration of lesion (Bq/ml)}}{\text{Average body radioactivity concentration (Bq / ml)}} \\ \text{(Dosage (Bq) / Weight (g))}$$

**The radioactivity of the numerator and denominator must be synchronized (with half-life correction).**

Semi-quantitative value indicating how many times the radioactivity concentration of the lesion is higher than the body average. The normal value is 1. 2.5 to 3 or more are considered pathological accumulation.

# 半減期 Half life $T_{1/2}$

$$N = N_0 \times (1/2)^{(t / T_{1/2})}$$

崩壊定数 Decay constant  $\lambda$

1秒間に原子核が崩壊する割合

Nuclear decay rate per second

$$dN/dt = -\lambda N$$

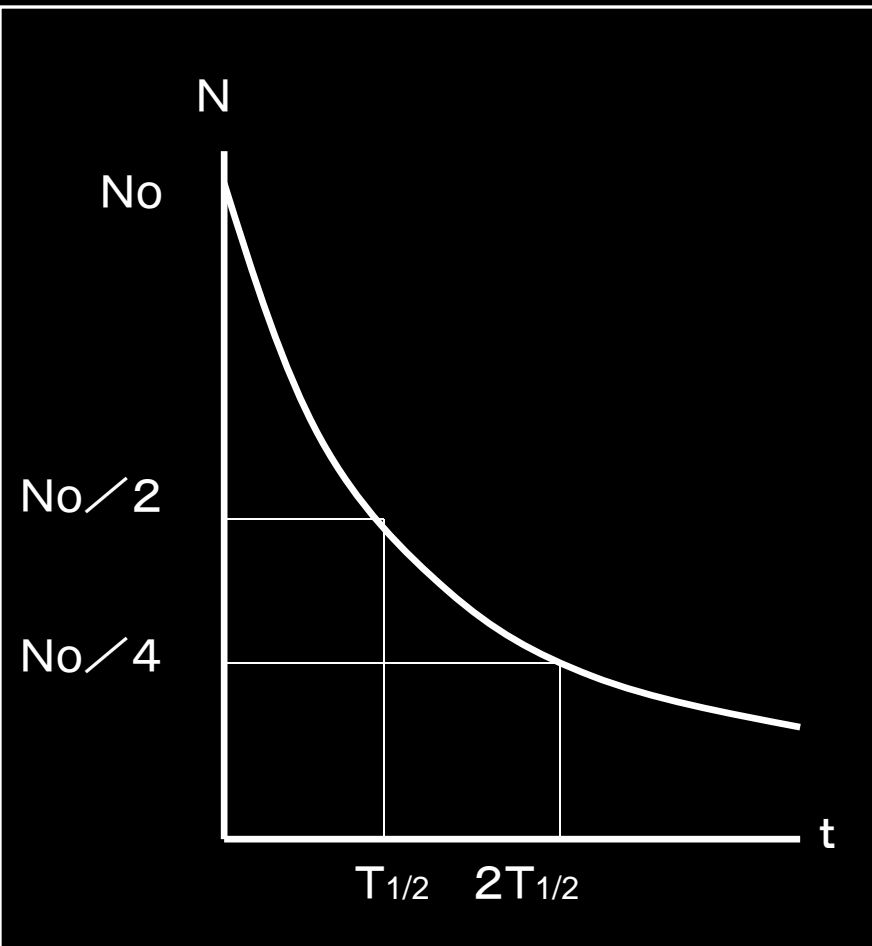
$$N = N_0 e^{-\lambda t}$$

$$N_0/2 = N_0 e^{-\lambda T_{1/2}}$$

$$1/2 = e^{-\lambda T_{1/2}}$$

$$\text{Log}(1/2) = \text{Log}(e^{-\lambda T_{1/2}})$$

$$\text{Log}2 = 0.693 = \lambda T_{1/2}$$



# Clinical Radiologist National Examination

$^{18}\text{F}$ -FDG that was 200 MBq at 10:00 was injected to a patient at 10:55. PET scanning was started at 11:50, and image analysis was performed at 13:40.

The radioactivity of the lesion was 12000 Bq/ml. Calculate the SUV of the lesion.

( The patient's weight is 50 kg, height is 150 cm, and half-life of  $^{18}\text{F}$  is 110 minutes.)

Calculate the radioactivity at 11:50 of the imaging start time.

The radioactivity in the patient is  $200 \times (1/2) = 100$  MBq

The average concentration in the body is  $100 \text{ MBq} / 50 \text{ kg} = 2000 \text{ Bq} / \text{ml}$

Then, SUV in the lesion is  $12000 / 2000 = 6.0$

(There is no quantitative unit for SUV. SUV is semi-quantitative.)

# 膵頭部癌 Panc. head ca.

FDG-PET after meal showed SUV 2.2 in the lesion.

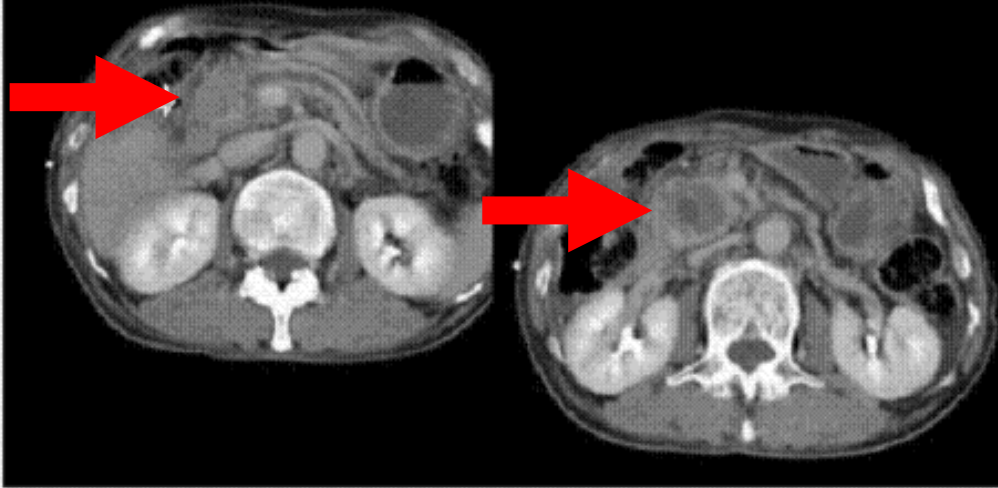
Re-study was performed on fasting, SUV in the lesion was raised to 3.4

FDG-PET must be performed in the fasting state.

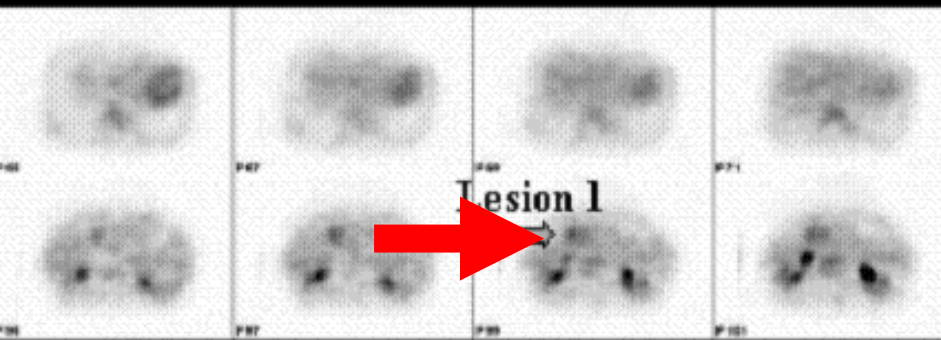
症例 3

CECT

(Contrast enhancement CT)



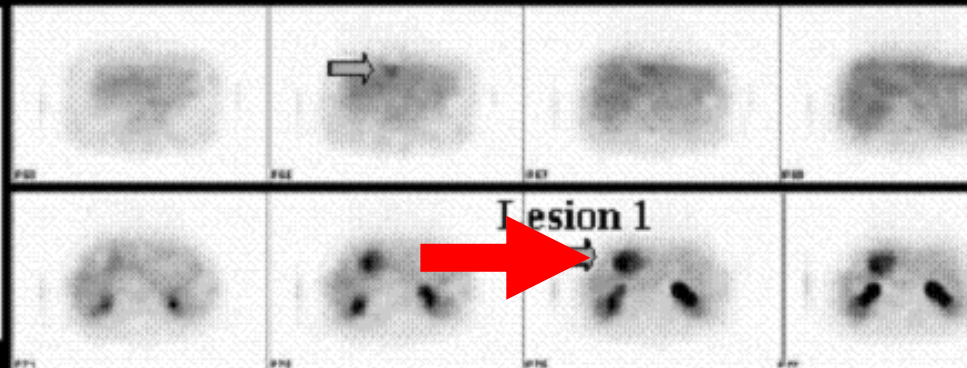
## 症例3: FDG-PET(1回目)



SUV 2.2 Lesion1 5029Bq/ml

前処置: 検査3時間前に食事(just after meal).  
検査時血糖 BS 167mg/dl

## 症例3: FDG-PET(2回目)



SUV 3.4 Lesion1 8251 Bq/ml

前処置: 検査前夜より絶食(fasted all night).  
検査時血糖95mg/dl

In the  $^{18}\text{F}$ -FDG PET study, the patient should be fasted and discontinued the sweet drink for 6 hours before. What is the problem with  $^{18}\text{F}$ -FDG PET study performed without the pretreatment ?

$^{18}\text{F}$ -FDG is an analog of glucose. Since glucose accumulates in tumors and inflammatory lesions, FDG also accumulates. Without fasting pretreatment, the patient's blood glucose level increases. In hyperglycemic conditions, tumors and inflammatory lesions accumulate much glucose, and FDG accumulation decreases due to the competition. Therefore, the uptake of the lesion on the PET image is reduced, and the SUV is also reduced. This makes it difficult to diagnose the lesion.



# Gamma camera

Equipment for imaging the distribution (scintigram) of gamma-ray emitting drugs in the body.



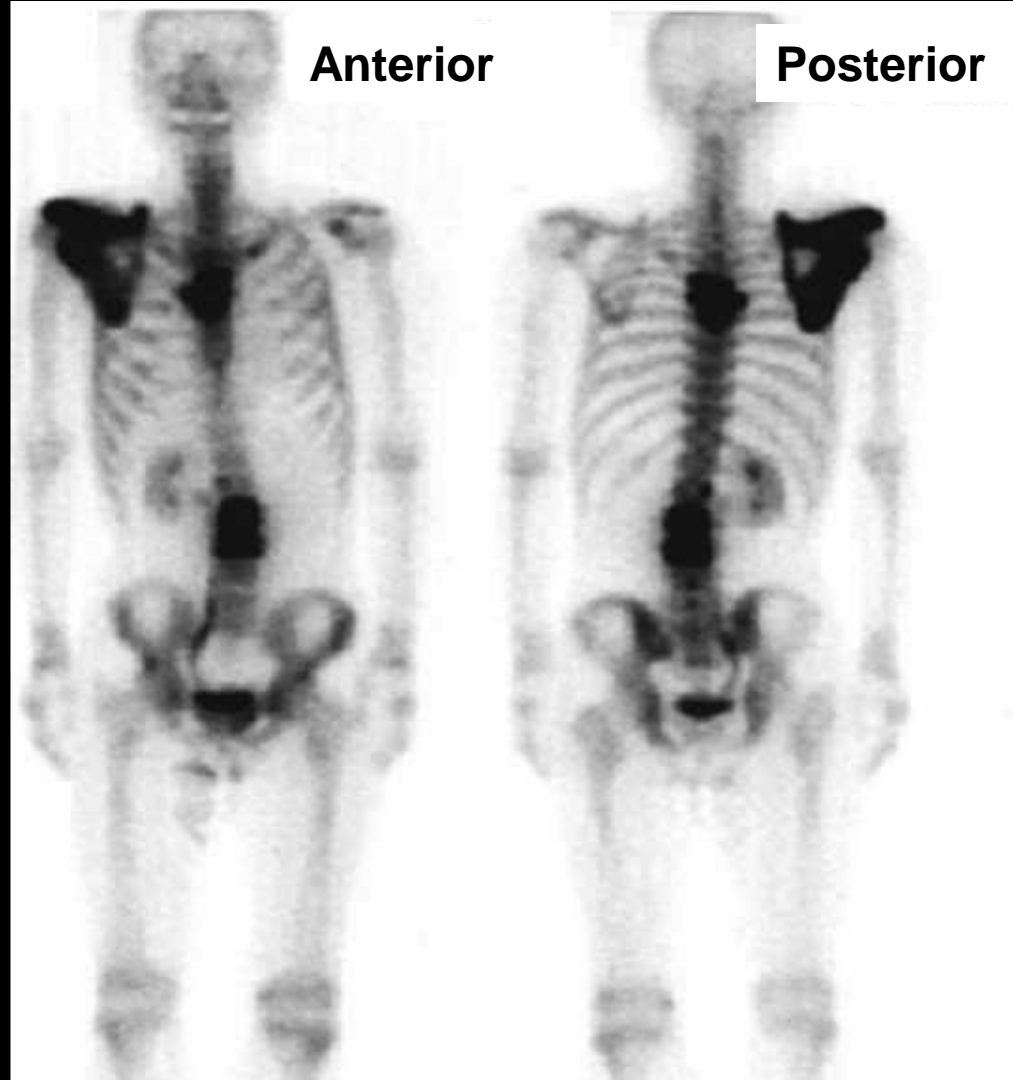
# 骨シンチグラフィ

## Bone scintigraphy

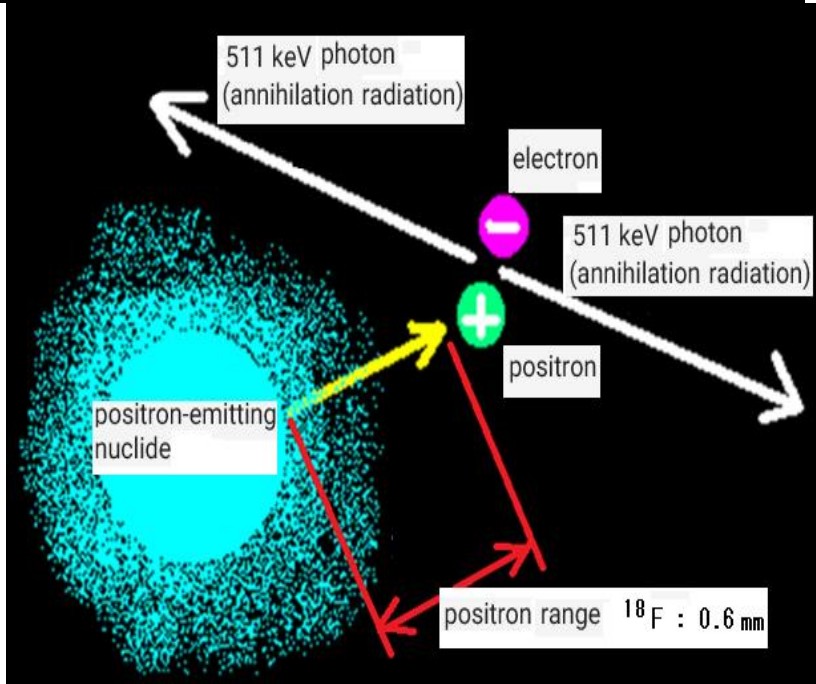
Distribution image of phosphoric acid labeled with gamma-emitting RI. Strongly distributed in bone metastatic lesions.

A case of lung cancer with bone metastasis in the right scapula, thoracic and lumbar spines.

Since this RI is excreted in urine much, the urinary tract and bladder are depicted.



The reason the images taken by the anterior and posterior cameras are different is that the human body absorbs and scatters gamma rays. The deeper the part from the body surface, the thinner the depiction.



## Annihilation

When a positron is emitted from the positron-emitting nuclide, it collides with the electron over a range of several millimeters and annihilates, and a pair of 511 keV annihilation radiation is emitted in the opposite direction.

The positron and the electron have the same mass, and when they annihilate, a photon (annihilation radiation) with a value of 511 keV is obtained by substituting the electron mass into the equation of  $E = mc^2$ .

! Electromagnetic waves generated from inside the nucleus are called  $\gamma$ -rays, and electromagnetic waves generated by the transition of extranuclear orbital electrons are called X-rays. Annihilation radiation is an electromagnetic wave that does not correspond to either.

! Positrons are antiparticles of electrons, having a positive charge and negative energy. When an electron and a positron whose energy and charge are opposite to each other meet, they disappear and are replaced by electromagnetic wave energy equivalent to the disappeared mass. Electromagnetic waves have no mass but energy, so they have momentum. The generated electromagnetic wave flies in the opposite direction according to the law of conservation of momentum. An accurate understanding of this phenomenon requires knowledge of quantum mechanics and relativity.

**There are two types of radiation.**

- 1. Electromagnetic waves (X rays,  $\gamma$  rays)  
= **Vibration energy of space****
- 2. Particle beam (electron, positron etc.)  
= Particle flying at high speed (with mass)  
which has greater effect on the human  
body than X-rays and gamma rays.**

**Radioactivity is the number of radiations  
emitted per second.**

**The unit of radioactivity is Becquerel (Bq).**

**Electromagnetic wave is the vibration energy of the space (X rays,  $\gamma$  rays, light rays, radio waves).**

**Space (or Universe) is not nothing.**

**The space has a physical entity (structure).**

**The vibration of the spatial structure becomes electromagnetic waves such as X-rays, gamma rays, visible light, etc.**

**Name and wavelength of electromagnetic wave**

X-rays and  $\gamma$ -rays: 10 pico to 10 nano-meters

Visible light : 400 (purple)–800 (red) nano-meters

Microwave: 100 micro to 1 meter

**Maxwell's formula : the speed of electromagnetic waves**

**Speed of electromagnetic waves in vacuum :**

$$C = 1 / \sqrt{\mu_0 \epsilon_0} = 300,000 \text{ km/s} = 3 \text{ billion m/s}$$

(  $\mu_0$  : Vacuum permeability ,  $\epsilon_0$  : Vacuum permittivity )

A vacuum (= space) has a structure having magnetic permeability and permittivity.

**= Space has a physical structure.**

If there is no structure in the space, the magnetic permeability  $\mu_0$  in vacuum (probability of magnetic field) and the dielectric constant in vacuum  $\epsilon_0$  (probability of electric field) should be zero.

If  $\mu_0 = 0$  and  $\epsilon_0 = 0$ , the electromagnetic wave velocity in vacuum  $C = 1 / \sqrt{\mu_0 \epsilon_0}$  should be infinite, which contradicts reality.



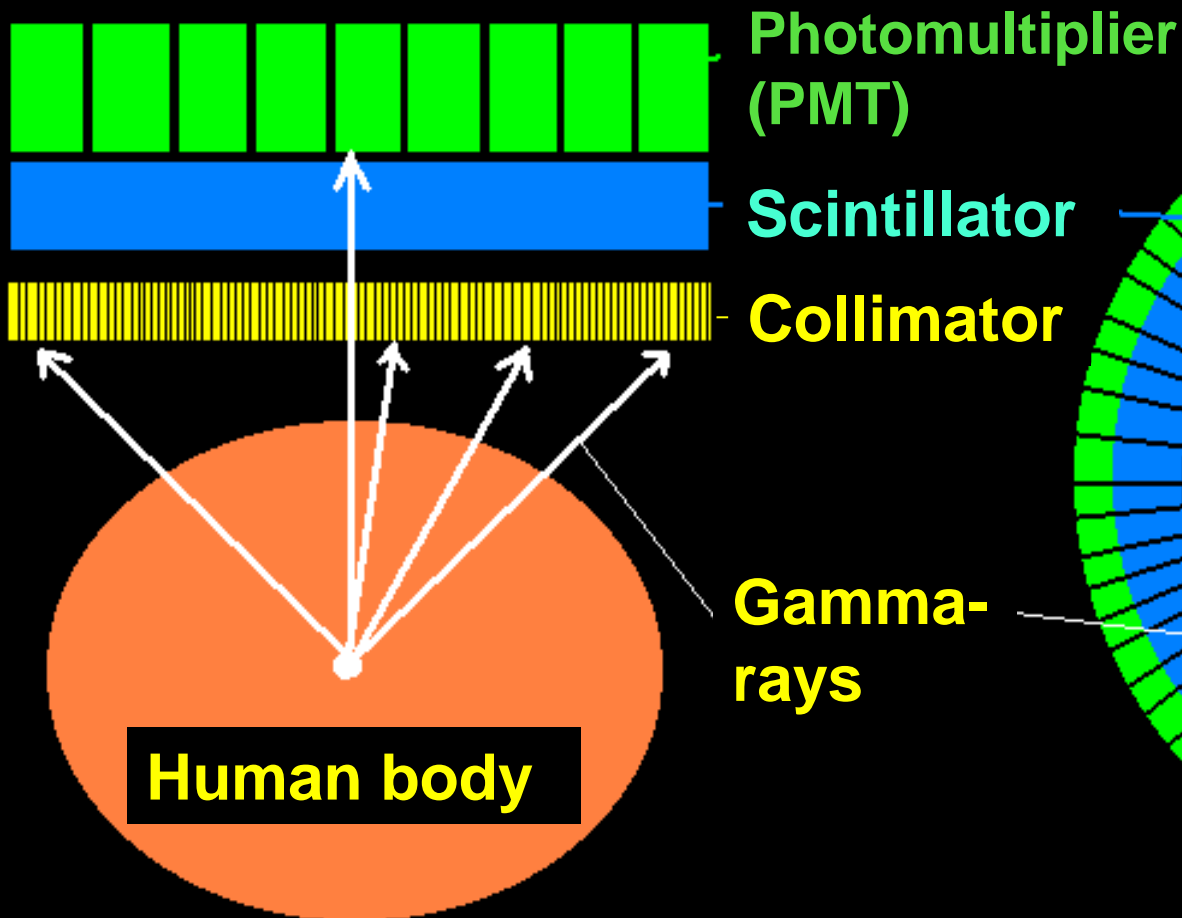
Photon is interpreted as a particle of energy in the space with zero weight. The particle feature of electromagnetic energy such as visible light or X-rays was confirmed by Einstein and Compton.

Even on a daily basis, the phenomenon that stars far from thousands of light years away can be seen in the night sky cannot be explained without recognizing the particle nature of light, that is, the existence of photons. If light is just a wave, the wave of light emitted from the star will spread for thousands of years in outer space, the energy of light reaching the earth will be significantly weakened, and we should not be able to see distant stars.

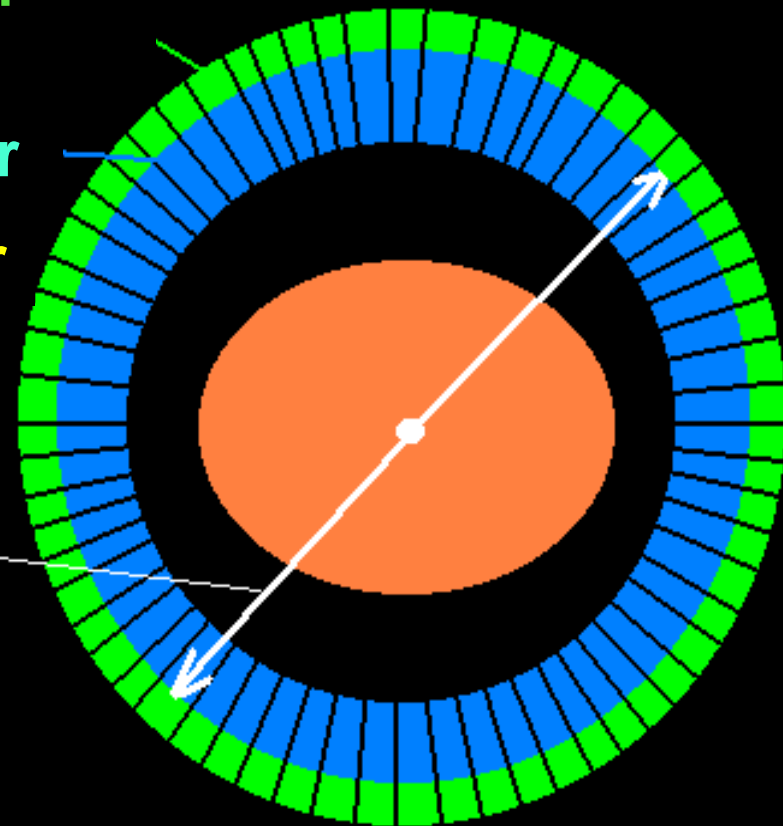
It is difficult to understand the duality that the electromagnetic energy has the feature of both wave and particle. The reason is that it is difficult for us to recognize space as a structure of four dimensions or more. If space has only three-dimensional structure, its duality cannot occur.

PET camera has high sensitivity because there is no collimator. The collimator mounted on the conventional gamma camera is a lead plate having many small holes. The collimator reduces the sensitivity of radioactivity detection.

## Conventional gamma camera

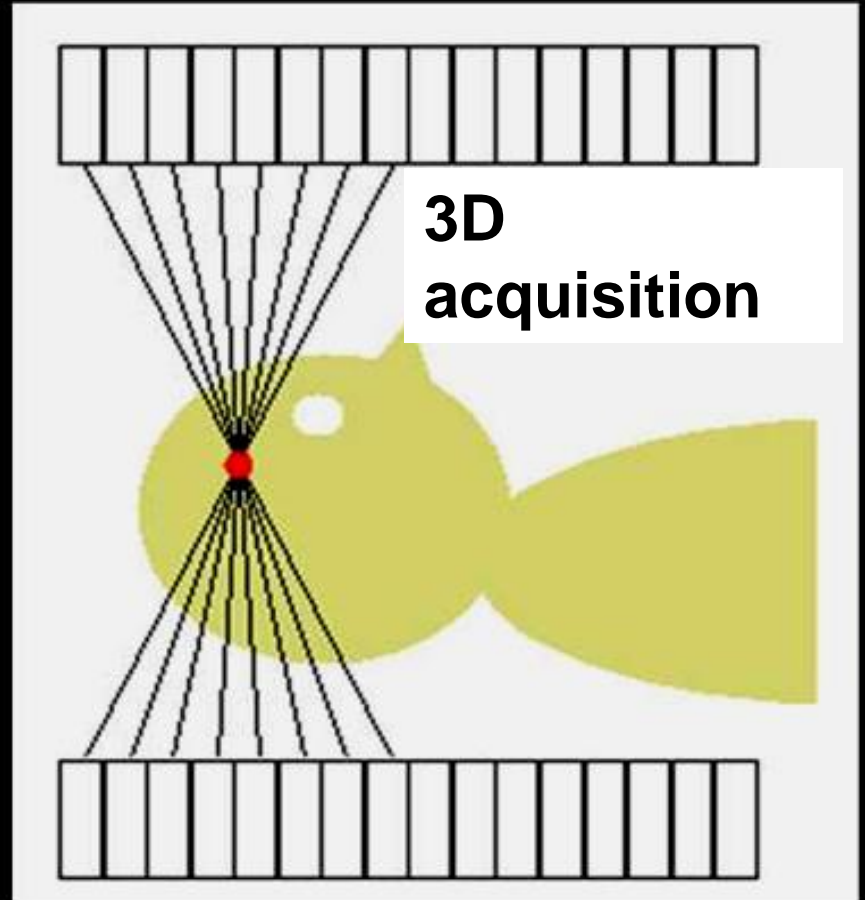
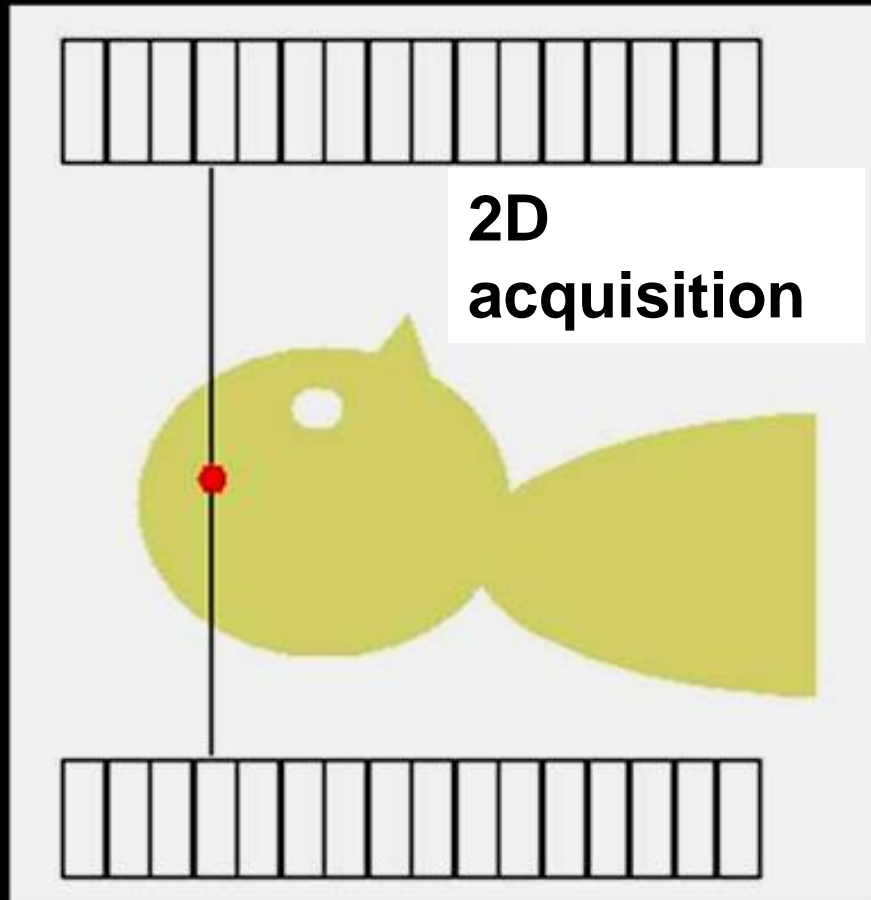


## PET camera



Currently, most PET is three-dimensional (3D) collection.

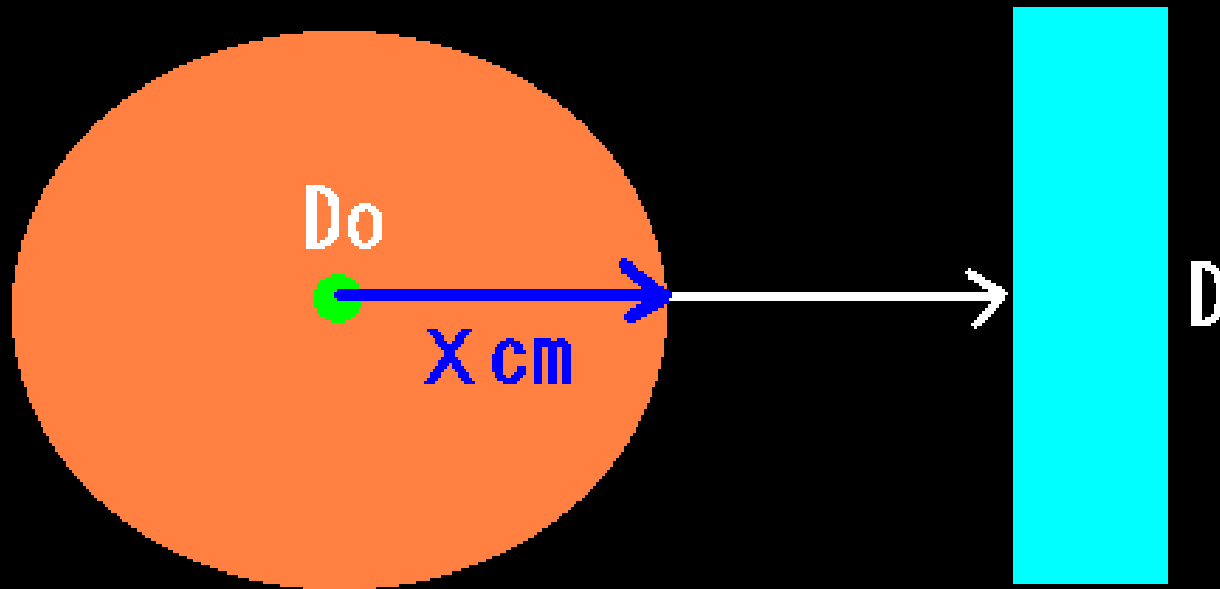
Good images can be acquired in a short time compared to two-dimensional (2D) acquisition (The whole body (head to thigh) is collected in about 15 to 20 minutes). But, it is easy to collect Compton scattered radiation, and the accuracy of quantification decreases.



# Difficulty quantifying radioactivity distribution in the body with conventional camera

Attenuation of radioactivity  $D_0$  in the body into  $D$

$$D = D_0 \exp(-\mu x)$$



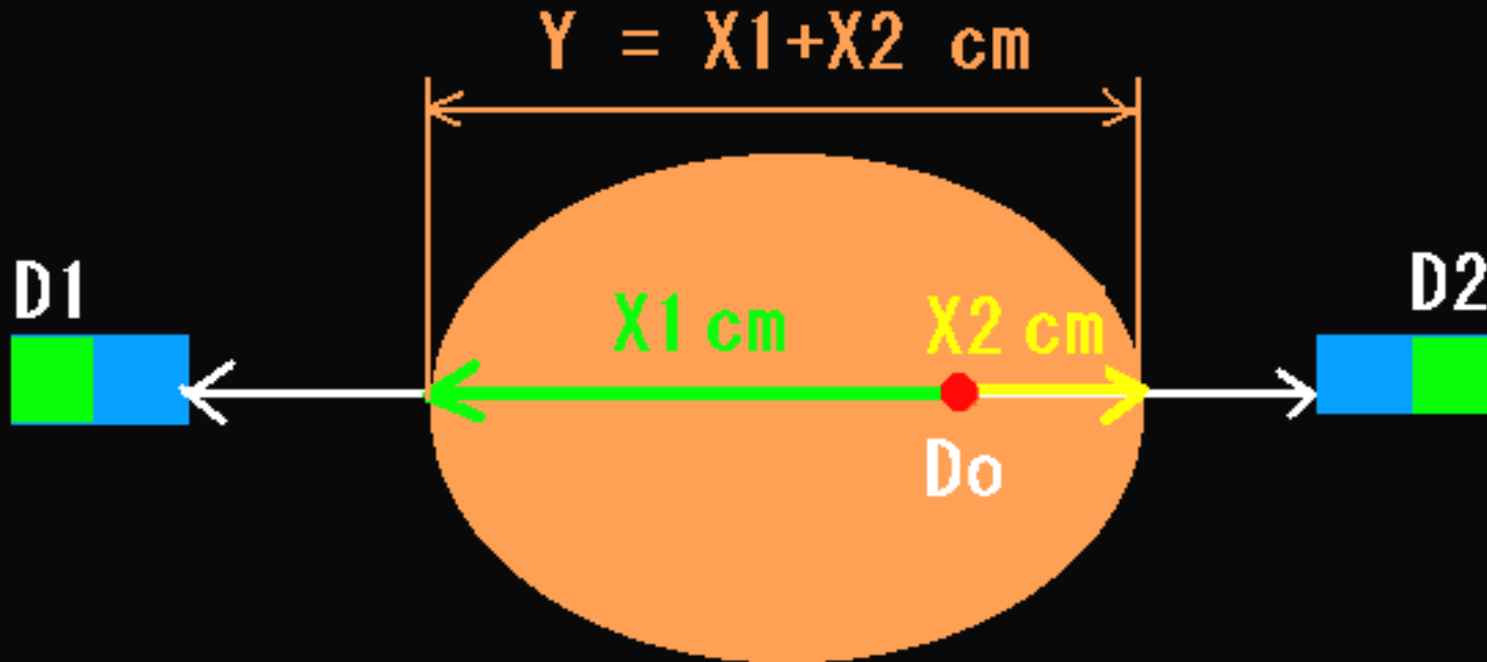
$D_0$  : True radioactivity (Bq)

$D$  : Measured radioactivity (Bq)

$\mu$  : Linear attenuation coefficient ( $\text{cm}^{-1}$ )

Scintillation  
camera

**PET performs absorption correction on CT images, so it is highly quantitative.**



$$D_1 = D_0 \exp(-\mu X_1)$$

$$D_2 = D_0 \exp(-\mu X_2)$$

$$D_1 D_2 = D_0 D_0 \exp(-\mu (X_1 + X_2))$$

$$D_0 = \sqrt{D_1 D_2 \exp(\mu Y)}$$

# PET/CT

# Rt. Lung cancer with metastases.

ファイル(E) 編集(E) 表示(B) 表示2 画像(O) マーク(D) 計測

視野条件

SUVの計算方法

体重

透過率	PET 比率	SUV 下限	SUV 上限
0.0	50	0.0	4.0

30 100% 00~120  
25 75% 00~100  
20 50% 00~80  
1.5 25% 00~60  
0.0 0% 00~4.0

プリセット編集

一覧表示

PET  
CORONAL MP

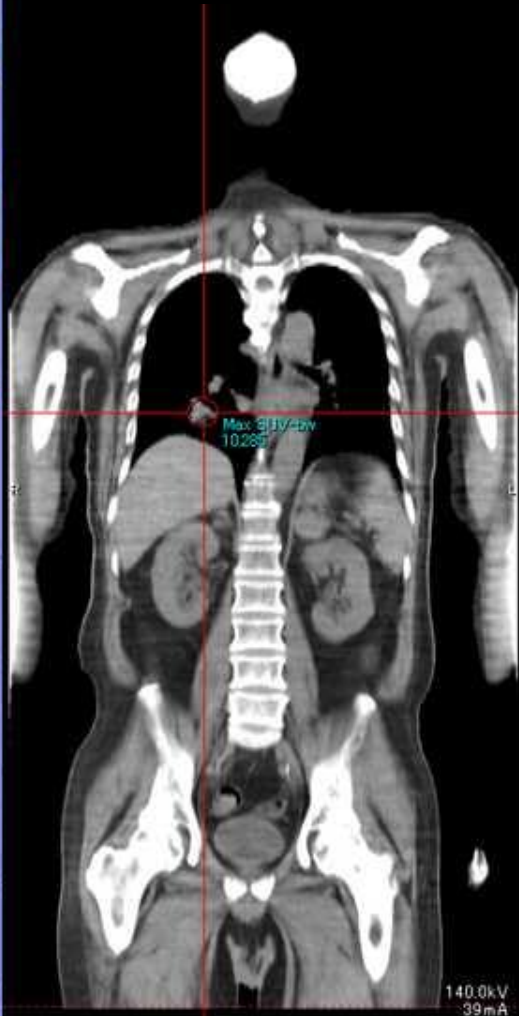
FUSION  
CORONAL

機能

SUV 関連情報表示  
球形 ROI 解析  
CT S/N比改善 設定  
カラーマップオーバーレイ選択

fi スケール

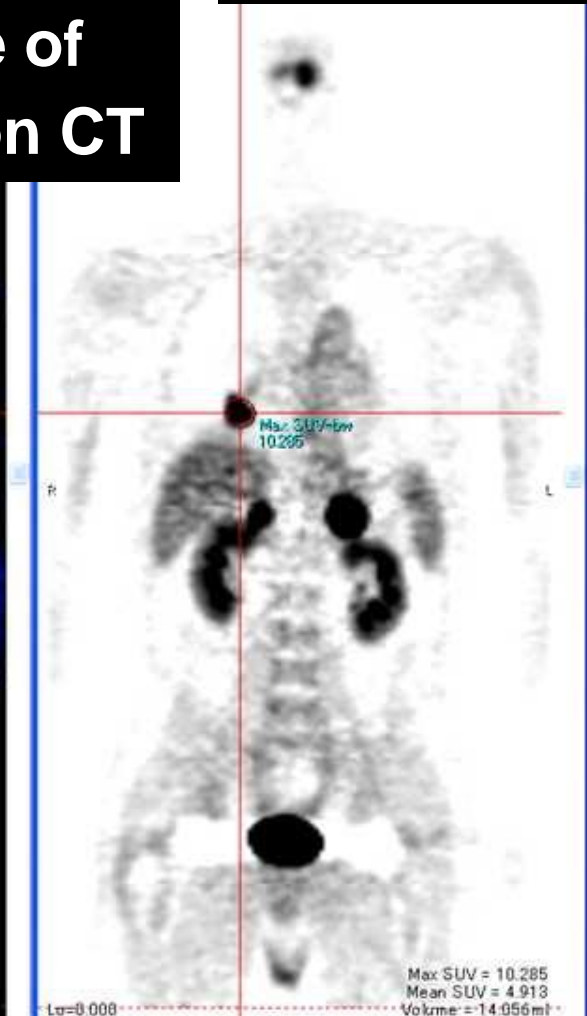
CT image  
 $\mu(x,y,z)$



Super-imposed image of PET on CT



PET image  
 $Do(x,y,z)$



**PET image ( $Do$ ) is generated using CT image ( $\mu$ ).**



# CT value ( HU : Hounsfield Unit )

Value proportional to tissue density

The value based on the pixel value of the CT tomogram is the linear attenuation coefficient  $\mu_t$  of each tissue in the body, but a value proportional to  $\mu_t$  is used for the pixel value of CT to facilitate clinical understanding.

$$\text{CT value} = 1000 \times (\mu_t - \mu_w) / \mu_w$$

$\mu_w$  : X-ray absorption coefficient in the water

$\mu_t$  : X-ray absorption coefficient in the tissue

## CT value in the air is -1000

$$1000 \times (\mu_{\text{air}} - \mu_w) / \mu_w = -1000 \text{ (HU)}$$

Strictly, the linear attenuation coefficient  $\mu_{\text{air}}$  is not 0. But it is extremely small compared to water or body tissue, when calculating the CT value,  $\mu_{\text{air}} = 0$ .

## CT Value in the water is 0 (HU).

( Density of specific gravity 1 is 0 (HU) )

$$1000 \times (\mu_w - \mu_w) / \mu_w = 0 \text{ (HU)}$$

The CT value of a substance with a linear attenuation coefficient twice that of water is 1000.

Double density of water is 1000 (HU). ( Tooth etc. )

$$1000 \times (2 \mu_w - \mu_w) / \mu_w = 1000 \text{ (HU)}$$

北大医学部 加藤千恵次 [北大病院 核医学診療科](#)

大学院医学研究科 [PETIによる病態の定量化](#) [断層画像再構成の原理](#)

医学科 核医学 [PET, SPECTの原理](#) [エンパートメントモデル解析](#)

保健学科

保健学科2年 保健医療概論 [原子力発電所事故が人体に与える影響](#)

[医療従事者の被曝について](#)

放射線技術科学専攻

[核医学総論](#) [核医学検査技術学](#)

[核医学検査技術学実習](#)

[放射化学基礎](#)

[放射線関係法規](#)

[医用画像機器工学II \(CT\)](#)

[医用画像機器工学実習 \(FBP, OSEMの原理\)](#)

[核医学機器工学概論](#) [プログラミング言語C](#)

[C#講座](#) [C#講座サンプルプログラム](#) [プログラミング言語C#](#)

[C言語からVisual C#への移行](#) [DICOMから情報を読み出す](#)

検査技術科学専攻

[医療情報科学](#) [医用工学](#)

# Take home message

[chtgkato.com](http://chtgkato.com)

Detailed nuclear medicine equipment principles, CT tomographic image creation principle, Slides explaining quantitative analysis theory such as cerebral blood flow, Image analysis programs.

Please refer to those who are interested.

# Positron emitting nuclides used in PET

Produced in a cyclotron in a hospital.

		Half-life	Synthetic radiopharmaceutical
酸素15	15-O	2 min.	O <sub>2</sub> , CO, CO <sub>2</sub> , H <sub>2</sub> O
窒素13	13-N	10 min.	NH <sub>3</sub>
炭素11	11-C	20 min.	<sup>11</sup> C-Acetate <sup>11</sup> C-Methionine
フッ素18	18-F	110 min.	FDG, FDOPA

## Half-life of radioisotopes used in conventional Nuclear medicine studies

- 99m-Tc 6 hours (時間)
- 67Ga 78 hours (時間) (3.2 days 日)
- 201Tl 73 hours (時間) (3.0 days 日)

$^{18}\text{F}$  110 min  
 $^{15}\text{O}$  2.04 min  
 $^{11}\text{C}$  20.4 min  
 $^{13}\text{N}$  9.97 min

$^{18}\text{O}(\text{p},\text{n})\ ^{18}\text{F}$   
 $^{14}\text{N}(\text{d},\text{n})\ ^{15}\text{O},\ ^{15}\text{N}(\text{p},\text{n})\ ^{15}\text{O}$   
 $^{14}\text{N}(\text{p},\alpha)\ ^{11}\text{C}$   
 $^{12}\text{C}(\text{d},\text{n})\ ^{13}\text{N},\ ^{16}\text{O}(\text{p},\alpha)\ ^{13}\text{N}$



## Cyclotron

A Cyclotron in Hokkaido University hospital.

Huge electromagnet.

Accelerates hydrogen or deuterium nuclei

and collides with elements to create positron emitting nuclides.

# 被曝 Exposure unit

**Absorbed dose** : 1 Gy (gray) is the exposure of a 1 kg object absorbing 1 J of radiation energy.

**Dose equivalent**: The exposure to which the human body receives 1 J of energy per 1 kg of body weight is 1 Sv.

**Dose equivalent (Sv) = Absorbed dose (Gy) x Quality factor**

**Quality factor Q** : An index that indicates the energy applied to the human body (the degree of ionization) due to differences in radiation quality.

**Q=1** : X-rays、 $\gamma$ -rays、 $\beta$ -rays

**Q=10** : Proton beam、neutron beam

**Q=20** : Multiple charged particles



Due to the short half-life of positron emitting nuclides, exposure to PET scans is low.

The unit of exposure is Sv ( $\text{mSv} = 0.001\text{Sv}$ ).

Exposure to receive 1J of energy per 1kg of body weight is 1Sv. Generally, 100mSv or less is harmless.

$^{18}\text{F}$ -FDG (185MBq) 4 mSv (Bladder 20 Heart 10 Fetus 3)

$^{11}\text{C}$ -Methionine (370MBq) 2 mSv (Pancreas, Liver 7)

$^{15}\text{O}$ -CO<sub>2</sub> (3000MBq) 2 mSv (Lung 11)

CT 7mSv ~ 10 ~

Angiography 7 mSv ~ 10 (Skin in 1 minute 0.5)

Stomach, digestive tract X-ray imaging 3 mSv

X-ray photography 0.1 mSv (Chest) 0.2 mSv (Pelvis)

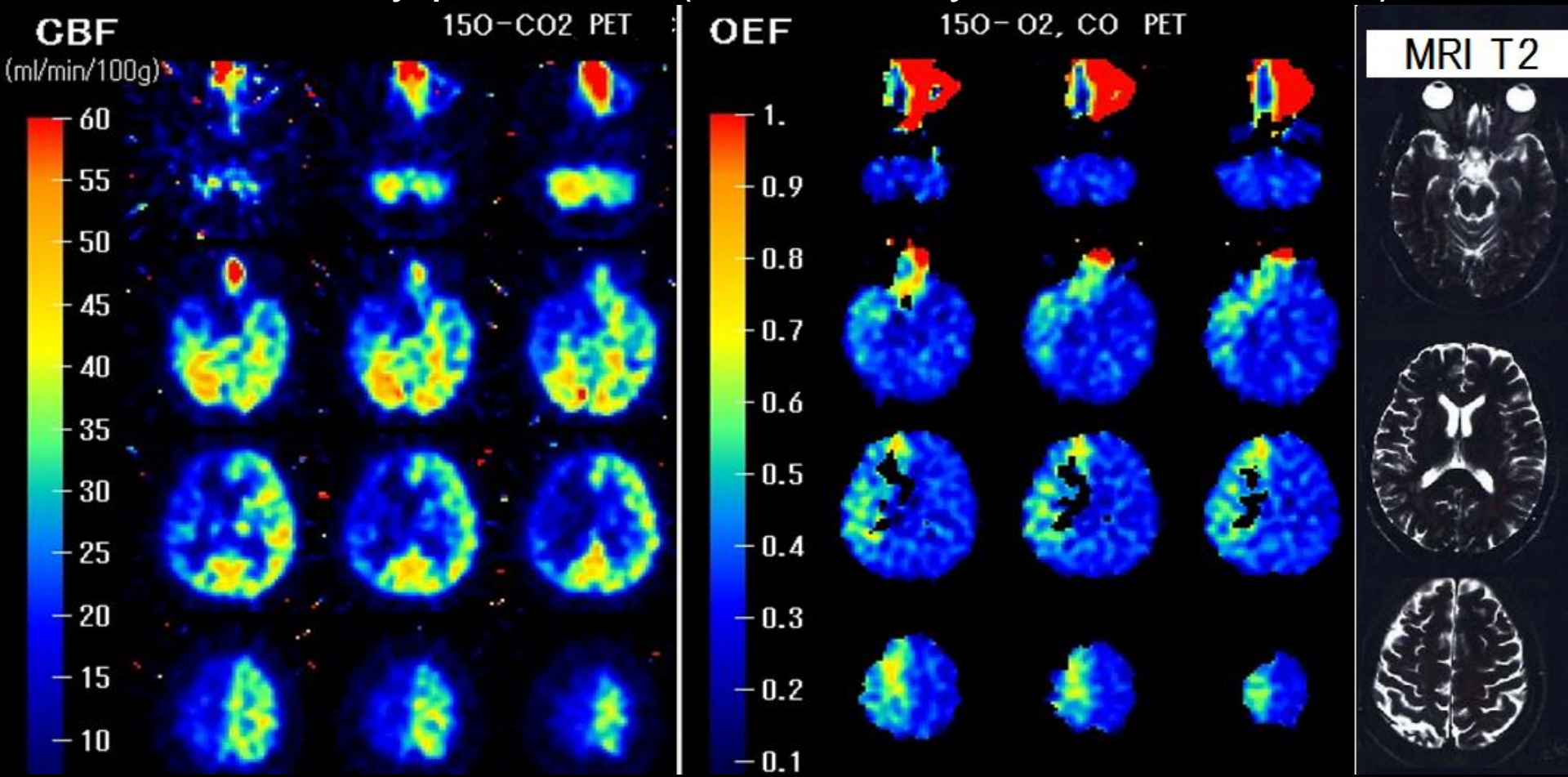
# $^{15}\text{O}\text{-CO}_2$ , $\text{O}_2$ Brain PET quantifies CBF, OEF.

## Cerebral Blood Flow (CBF), Oxygen Extraction Fraction (OEF).

Case of severe stenosis in the right internal carotid artery.

Although it is not a cerebral infarction (MRI T2 image is normal), severe hypoperfusion, increased oxygen uptake in the Rt. brain.

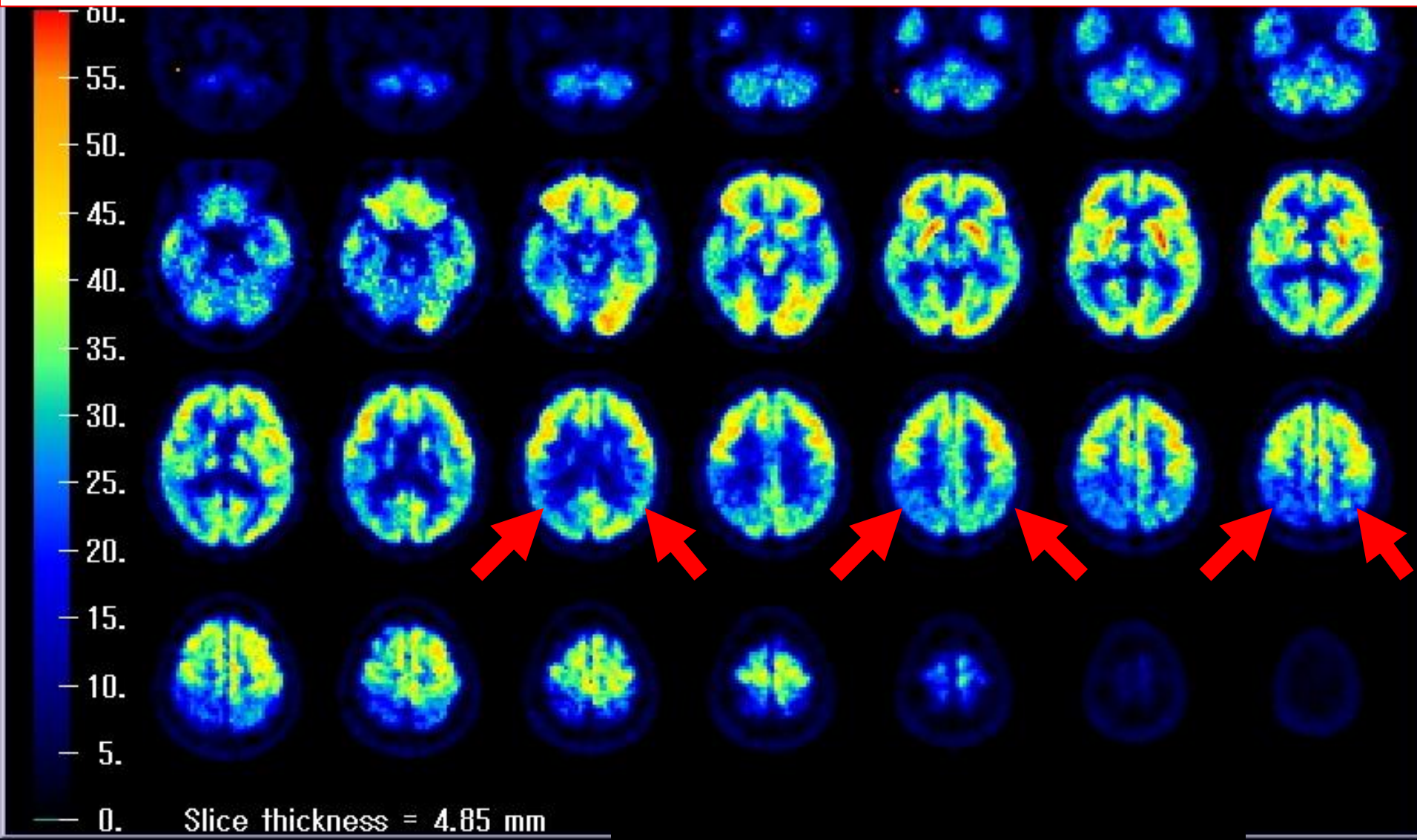
It is called misery perfusion. (Immediately before infarction )



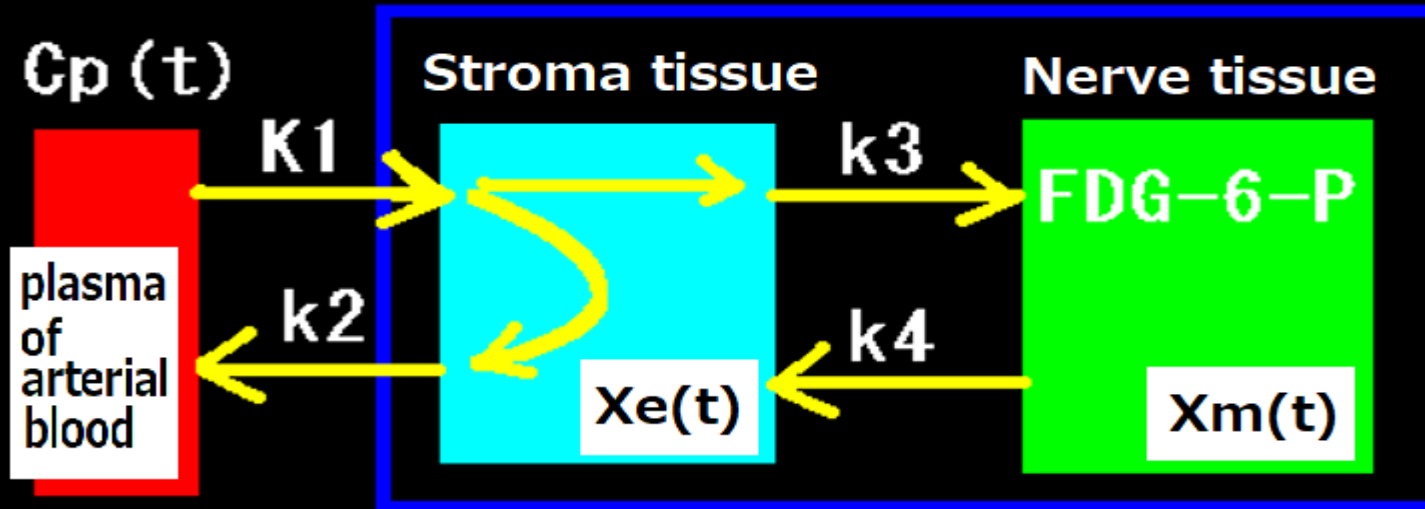
**$^{18}\text{F}$ -FDG Brain PET Quantify brain glucose consumption.**

**Alzheimer's disease**

**Degeneration of bilateral parietal and temporal lobes,  
decreased glucose metabolism.**



# Quantitative analysis of dynamic FDG PET with three-compartment model



$$\frac{dC_p}{dt} = k_2 X_e - K_1 C_p$$

$$\frac{dX_e}{dt} = K_1 C_p + k_4 X_m - (k_2 + k_3) X_e$$

$$\frac{dX_m}{dt} = k_3 X_e - k_4 X_m$$

CMRGlc (Cerebral Metabolic Rate of Glucose)

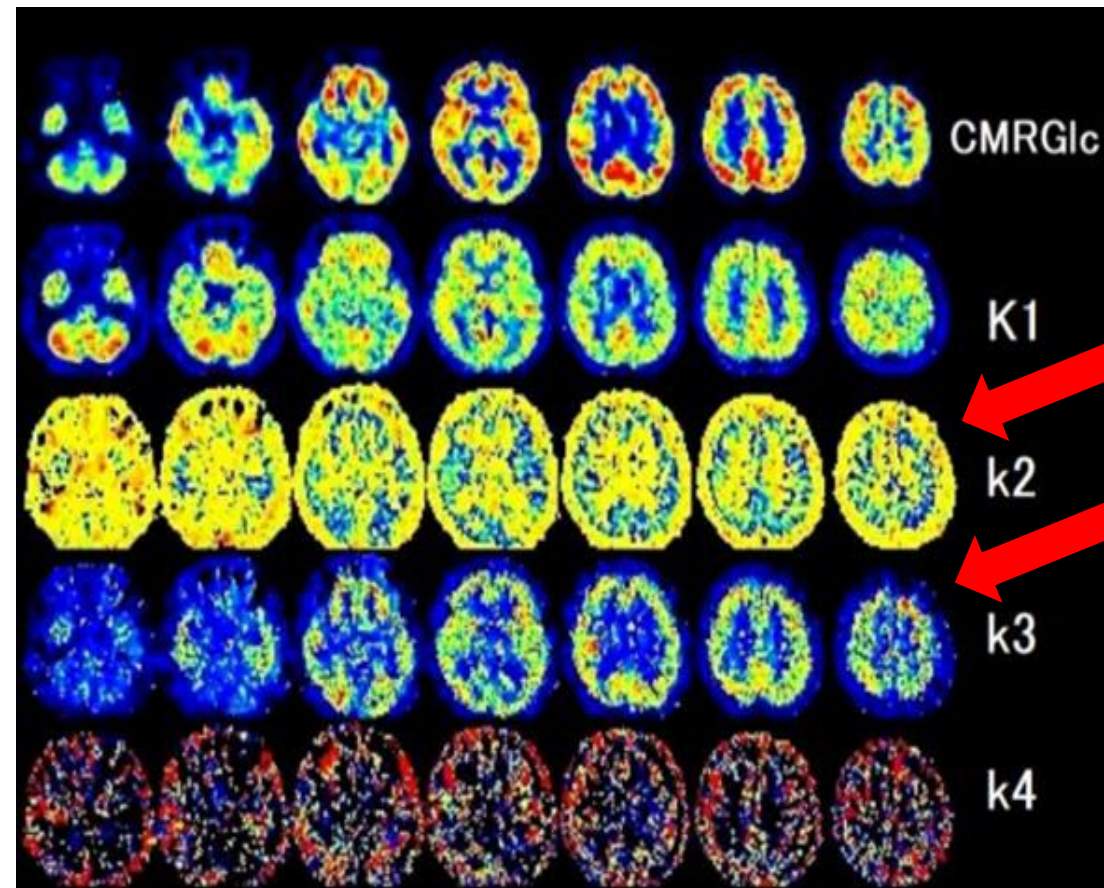
$$= \frac{\text{Blood sugar} \times K_1 \times k_3 / (k_2 + k_3)}{0.42}$$

0.42 is a Lumped constant, uptake ratio of FDG compared with Glucose.



**3-compartment model analysis enables to calculate rate constant images of  $K_1$  ,  $k_2$ ,  $k_3$  and  $k_4$  from dynamic FDG PET image and arterial blood sampling.**

**$K_1$  image shows uptake rate of FDG into both stroma and nerve tissues.**



$k_2$  images show release rate of FDG from stroma tissues.

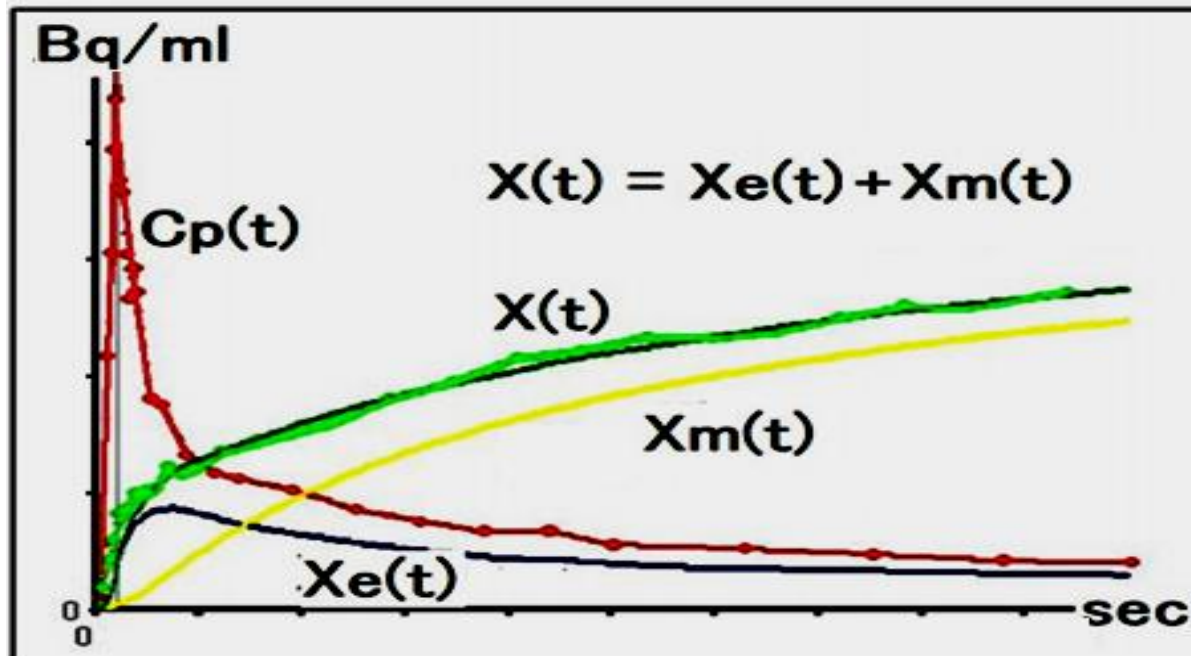
Stroma tissues do not need Glucose, high  $k_2$  value is shown.

$K_3$  images presents uptake rate of Glucose into the nerve tissues.

Nerve tissues need Glucose, high  $k_3$  value is shown in the brain.

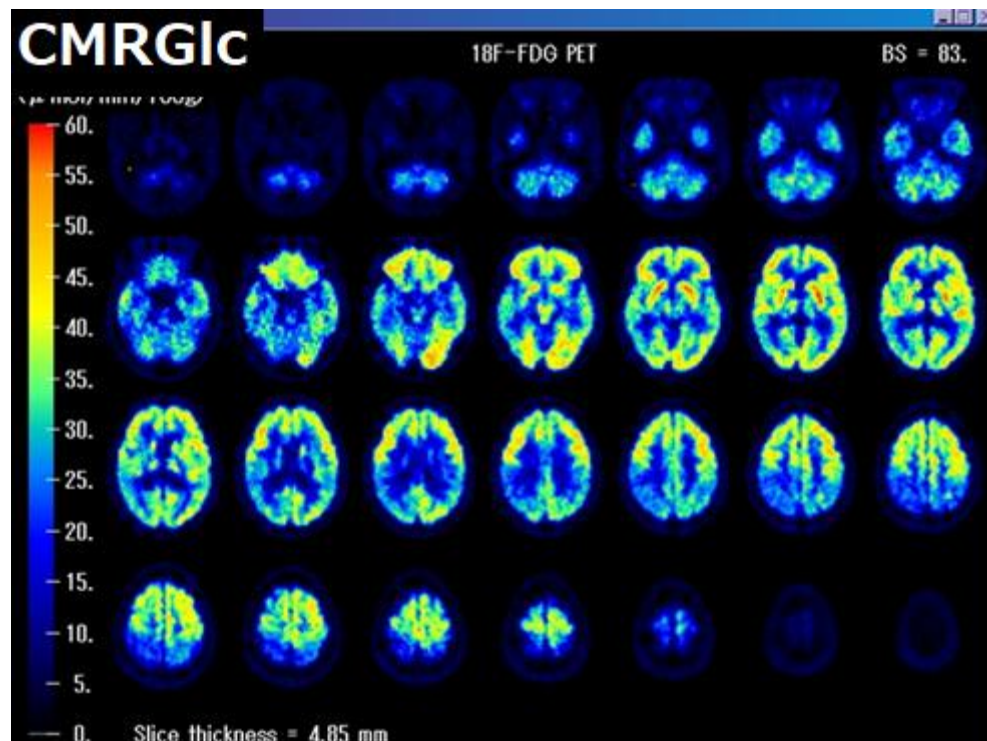
Dynamic brain FDG PET is performed for one hour, time-activity curve  $X(t)$  is acquired in every part of the brain.

3-compartment model analysis enables to divide the  $X_1$  curve into the 2 time-activity curves,  $X_e(t)$  (stroma tissue curve) and  $X_m(t)$  (brain tissue curve). This technique enables to analyze several pathological uptake rate of brain nerve tissues.



**Compartment model analysis is very useful to analyze quantitative evaluation of several diseases. But it sometimes requires arterial blood sampling during the dynamic PET acquisition.**

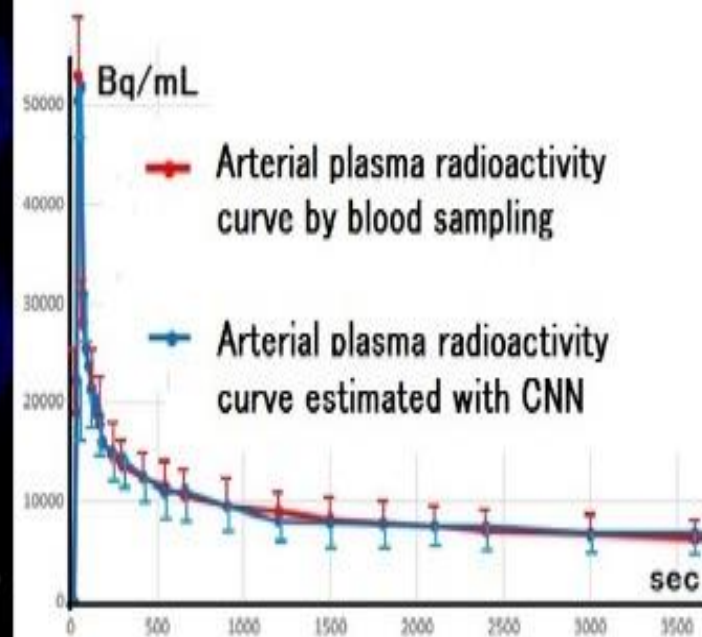
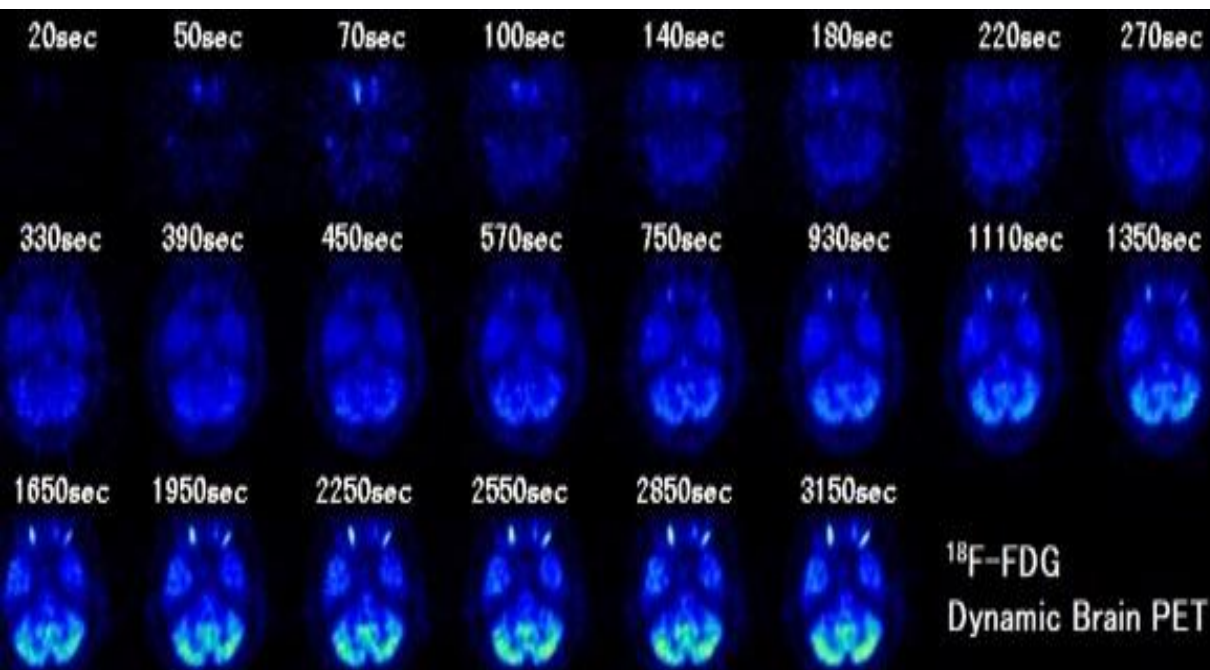
**It is invasive and expose high radiation to the doctor who is sampling blood, because he must be nearby a patient who is emitting gamma rays from the body.**





Recently, Deep-Learning is used in the clinical study. Several cases of  $^{18}\text{F}$ -FDG dynamic brain PET data and time-activity curves of sampled arterial plasma were used as training data.

Then, the trained Deep-Learning algorithm could estimate the time-activity curve of arterial plasma. It enables non-invasive compartment model analysis.

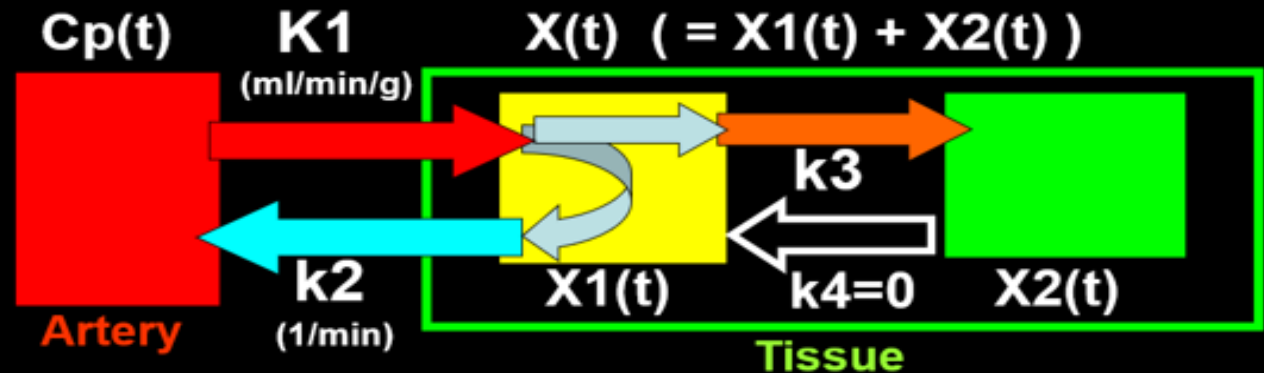


Patlak plot is a 3-compartment model analysis without arterial blood sampling.

This method is used clinically in the  $^{99m}\text{Tc-ECD}$  brain dynamic scintigraphy to estimate blood flow in the bilateral cerebral hemisphere.

Simplified model is used,  $k_4$  is assumed to be zero, formula of Patlak plot is derived.

### 3 Compartment model analysis ( case $k_4 = 0$ )



$$\frac{d X_1(t)}{d t} = K_1 C_p(t) - (k_2 + k_3) X_1(t)$$

$$\frac{d X_2(t)}{d t} = k_3 X_1(t)$$

$$K_i = K_1 \frac{k_3}{k_2 + k_3}$$

$$V_d = \frac{K_1}{k_2} \left( \frac{k_2}{k_2 + k_3} \right)^2$$

formula of Patlak plot

$$\frac{X(t)}{C_p(t)} = K_i \cdot \frac{\sum C_p}{C_p(t)} + V_d$$

$C_p(t)$  is a time-activity curve of the arterial plasma.  
 But clinically, in the  $^{99m}\text{Tc}$ -ECD dynamic brain scintigraphy,  
 the  $C_p(t)$  is used the time-activity curve of the Aortic arch.  
 $X(t)$  is time-activity curve of the bilateral cerebral hemisphere.

Distribution of  $\sum C_p(t) / C_p(t)$  and  $X(t) / C_p(t)$  are plotted,  
 a fitted line is drawn.

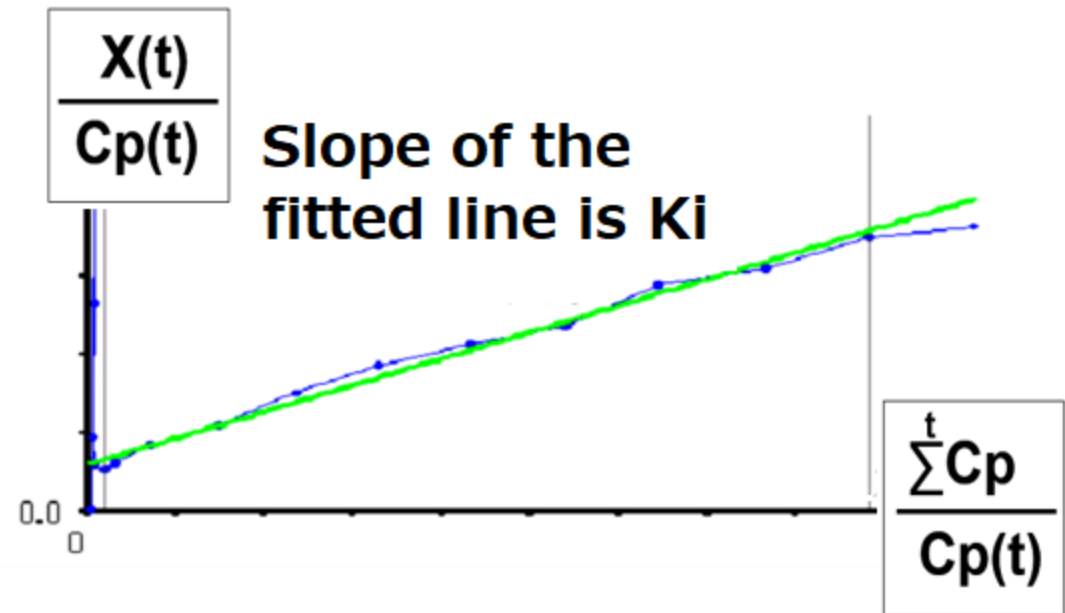
The slope of the line is

$$K_i (= K_1 \cdot k_3 / (k_2 + k_3))$$

$K_i$  means the uptake rate of  $^{99m}\text{Tc}$ -ECD into the cerebral hemisphere, the value is used as the cerebral blood flow.

formula of Patlak plot

$$\frac{X(t)}{C_p(t)} = K_i \cdot \frac{\sum C_p}{C_p(t)} + V_d$$



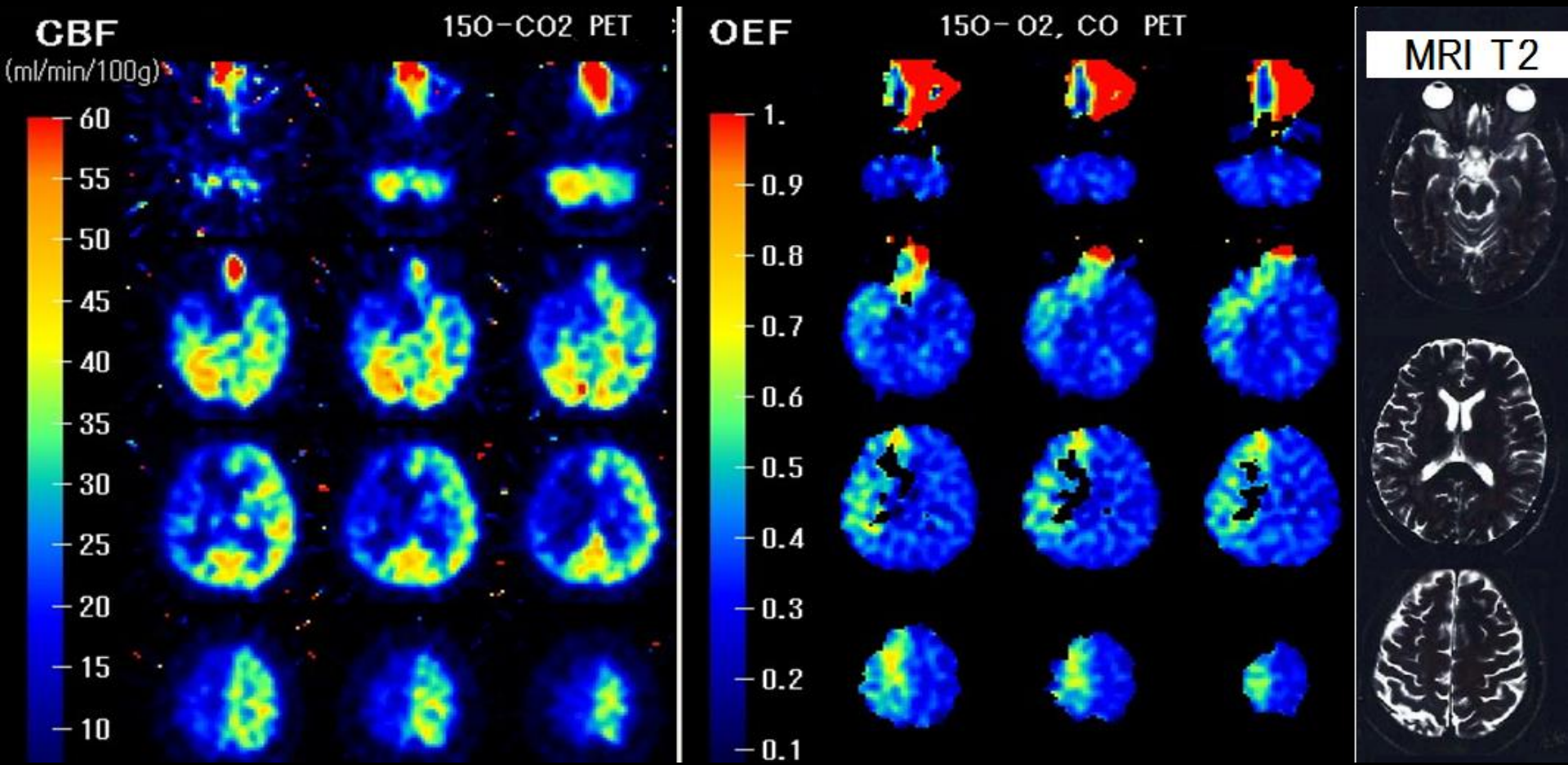
# $^{15}\text{O}\text{-CO}_2$ , $\text{O}_2$ Brain PET quantifies CBF, OEF.

## Cerebral Blood Flow (CBF), Oxygen Extraction Fraction (OEF).

Case of severe stenosis in the right internal carotid artery.

Although it is not a cerebral infarction (MRI T2 image is normal), severe hypoperfusion, increased oxygen uptake in the Rt. brain.

It is called misery perfusion. (Immediately before infarction )



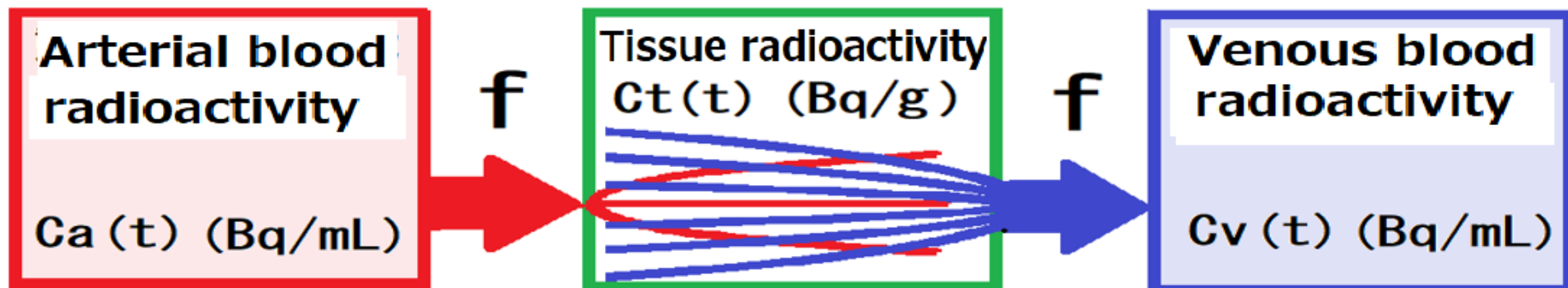


# Fick's principle

PET study using  $^{15}\text{O-CO}_2$  or  $^{15}\text{O-H}_2\text{O}$ , Fick's principle is used to estimate the tissue blood flow.

A micro-tissue uptakes  $C_t(t)$  of radioactivity during one second, and radioactivity of the artery and vein nearby the tissue are  $C_a(t)$  and  $C_v(t)$ , the relationship of  $C_t$ ,  $C_a$ ,  $C_v$  and blood flow of the micro-tissue  $f$  is presented as follows;

$$d C_t / dt = f (C_a - C_v)$$



**But it is impossible to measure the radioactivity of the vein nearby the micro-tissue  $C_v(t)$ .**

**Anatomically, the volume of venous blood is much larger than that of arterial blood in the micro-tissue.**

**So, radioactivity of the venous blood  $C_v$  and nearby microtissue  $C_t$  have a linear relationship.**

**Then the ratio of the  $C_t$  and  $C_v$  is defined the value  $p$  (partition coefficient ( $= C_t / C_v$ )). ( $C_v = C_t / p$ ).**

**The Fick's principle is presented as follows;**

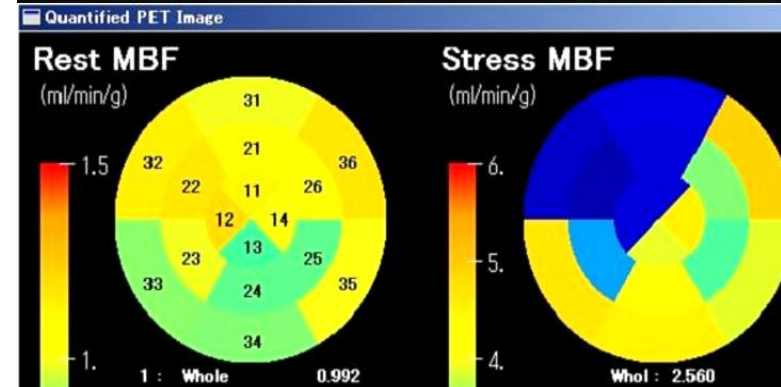
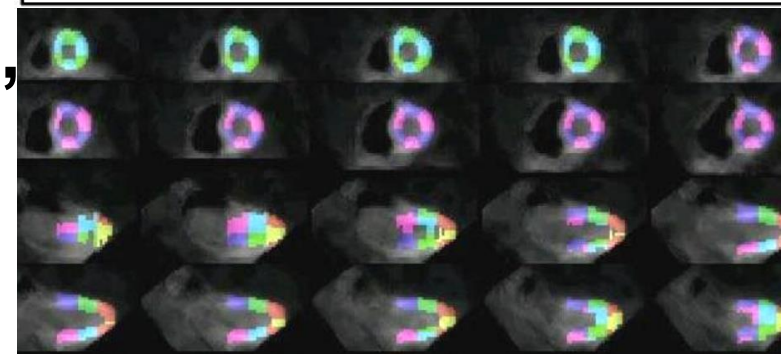
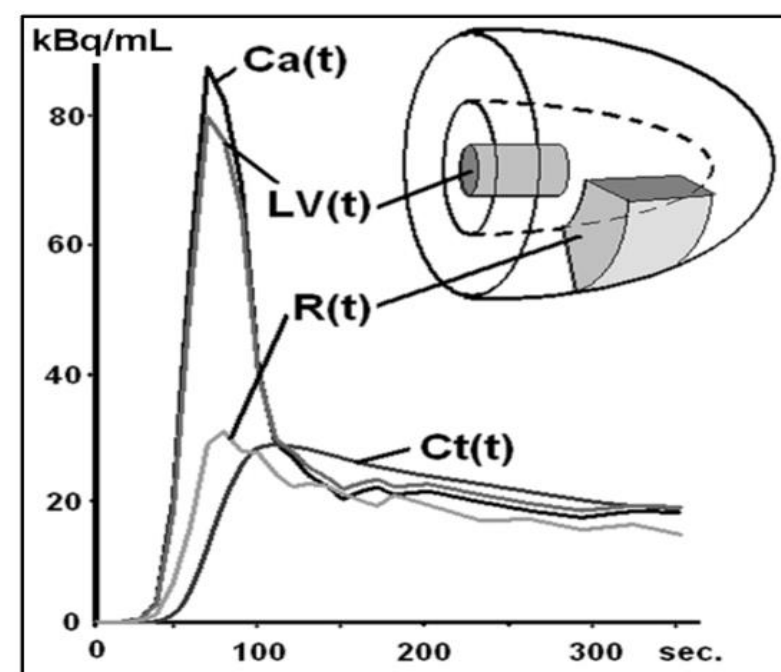
$$\mathbf{d C_t(t) / dt = f C_a(t) - (f / p) C_t(t)}$$

**This equation enables to estimate the tissue blood flow  $f$ , when  $C_a(t)$  and  $C_t(t)$  were acquired using dynamic PET study.**

**Myocardial PET study with  $^{15}\text{O}\text{-H}_2\text{O}$ , which enables to estimate regional myocardial blood flow (MBF) using Fick's principle.**

**In the heart study, radioactivity of the artery is derived from the Left ventricular count, blood sampling is not needed.**

**This case shows normal MBF at resting state, but decreased MBF at the LAD region at stressed state (ATP infusion). Effort Angina at LAD region is diagnosed quantitatively.**



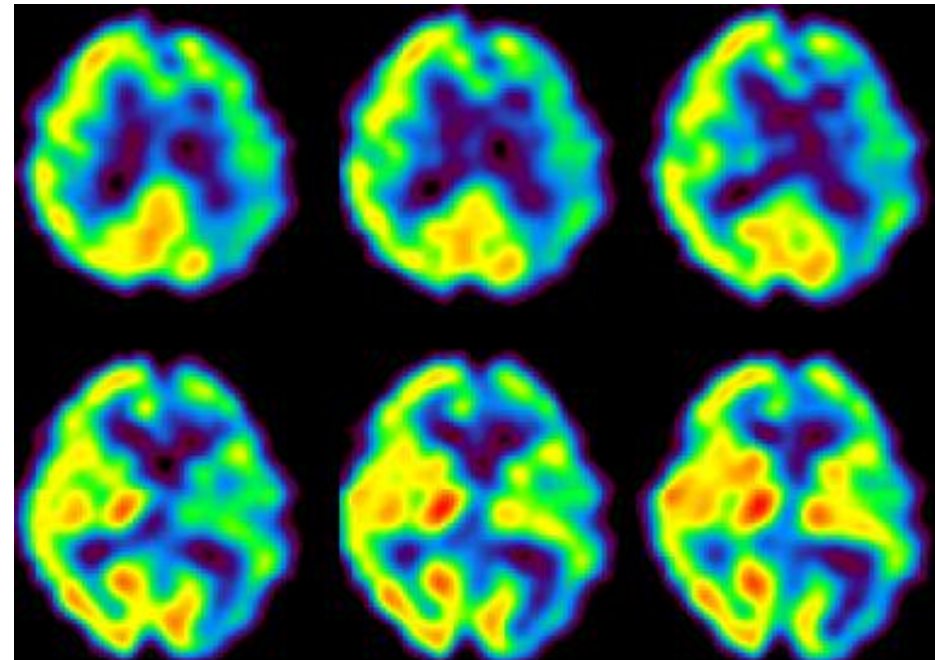
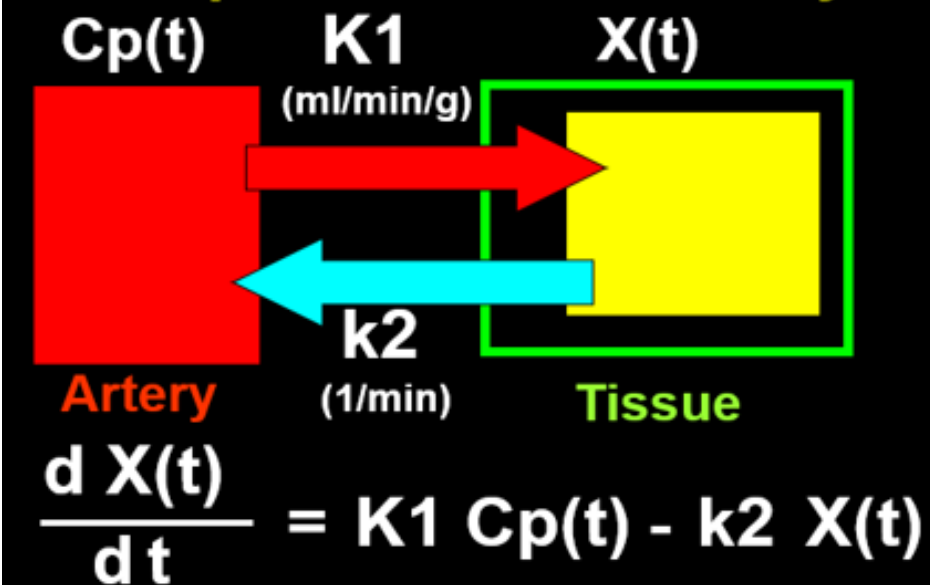


2-compartment model analysis is also useful. It is used clinically for the  $^{123}\text{I}$ -IMP Brain SPECT, myocardial dynamic PET with  $^{11}\text{C}$ -acetate,  $^{13}\text{NH}_3$ ,  $^{82}\text{Rb}$ .

## $^{123}\text{I}$ -IMP Brain SPECT

IMP is amphetamine, stimulant, highly accumulated into the brain nerve tissue. In the 2-compartment model,  $k_2$  (return rate from the brain to the blood) of IMP is assumed to be zero.

### 2 Compartment model analysis



When the  $k_2$  value is zero, 2-compartment model to estimate cerebral blood flow (CBF) is solved easily.

$$\frac{dX(t)}{dt} = K_1 C_p(t) \quad X(T) = K_1 \int_0^T C_p(t) dt$$

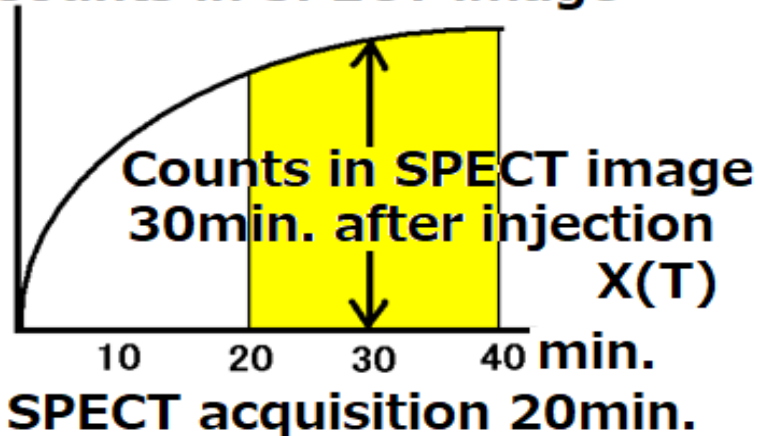
$$K_1 \doteq CBF = X(T) / \int_0^T C_p(t) dt \quad (T=30\text{min})$$

Radioactivity of the brain tissue in the SPECT image

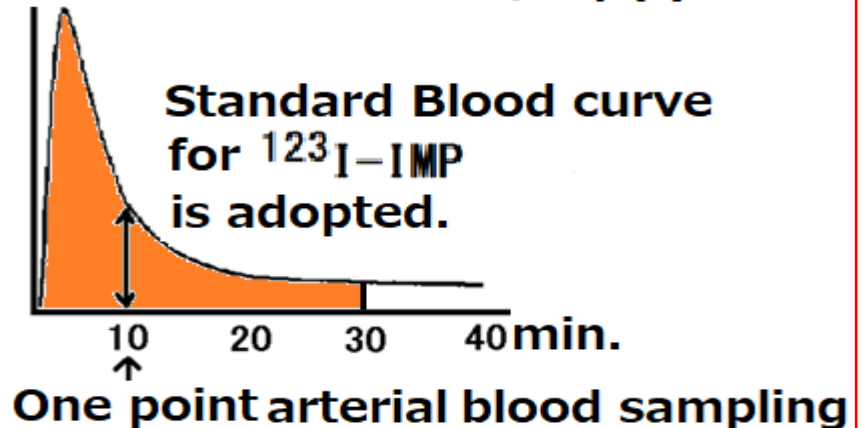
Integration of radioactivity of arterial blood for 30min.

$^{123}\text{I}$ -IMP Brain SPECT image is started to scan 20minutes after injection of  $^{123}\text{I}$ -IMP, acquisition time is 20minutes. So,  $^{123}\text{I}$ -IMP Brain SPECT is assumed to be scanned 30min. after injection.

Counts in SPECT image



Arterial Blood activity  $C_p(t)$



## Q.1

Which is correct about SUV of  $^{18}\text{F}$ -FDG PET ?

1. High blood sugar increases in tumors
2. Lower in muscles after exercise
3. Leakage of injection increases in the brain
4. One hour after administration, it becomes constant in the tumor
5. It becomes 1 when  $^{18}\text{F}$ -FDG is evenly distributed in the body.

## Q.2

Which lesion has low  $^{18}\text{F}$ -FDG accumulation ?

1. Colorectal cancer
2. Malignant melanoma
3. Malignant lymphoma
4. Head and neck squamous cell carcinoma
5. Well-differentiated hepatocellular carcinoma

Q.3

Choose two values to calculate SUV of  $^{18}\text{F}$ -FDG PET.

1. Weight
2. Blood glucose level
3. Radioactivity in blood
4. Volume of drug administered
5. Radioactivity of administered drug

Q.4

In the healthy person, which organ has less  $^{18}\text{F}$ -FDG accumulation?

1. Brain
2. Liver
3. Gall bladder
4. Kidney
5. Colon

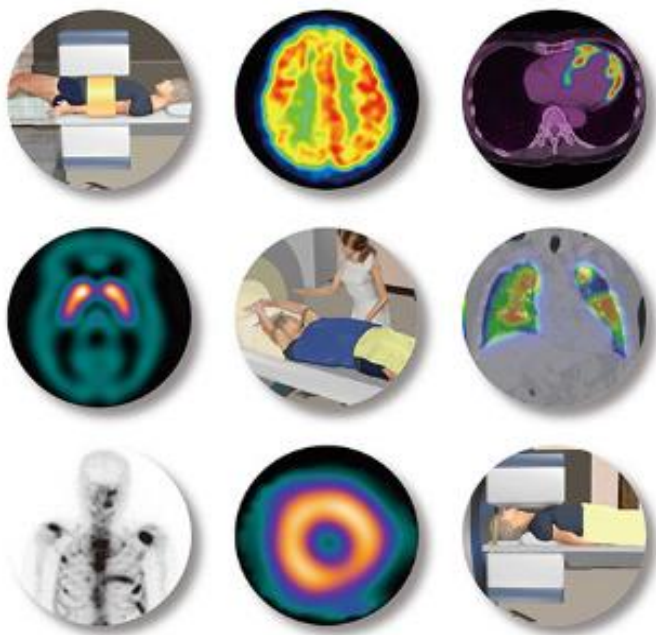
# References

フルカラーCGで学ぶ

## 核医学検査の テクニック

Techniques for Nuclear Medicine Imaging with Full-color Computer Graphics

監修 加藤千恵次 北海道大学 大学院保健科学研究院 医用生理工学分野 教授  
編集 孫田恵一 北海道大学病院 医療技術部(放射線部) 副診療放射線技師長  
編集協力 杉森博行 北海道大学 大学院保健科学研究院 医用生理工学分野 准教授



MEDICAL VIEW

フルカラーCGで学ぶ

## 核医学検査のテクニック

■監修

加藤 千恵次

■編集

孫田 恵一

■編集協力

杉森 博行

定価 6,050 円(税込) (本体 5,500 円+税)

B5判 288ページ オールカラー, イラスト170点

2020年3月2日刊行

ISBN978-4-7583-2019-1